

Rendering Competition Theme

- **Four rendering competition themes**
- **Vote for your favorite before *Sunday 23:59*
*December 3rd***
- **Think about the scene you want to render and how it could fit together with the theme you vote for.**

Vote for your favorite!

Journey to the Unknown

Whispers of Tomorrow

Chaos in Harmony

Lost in Translation

Computer Graphics

- Texturing -

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Alexander Rath
Philipp Slusallek

Overview

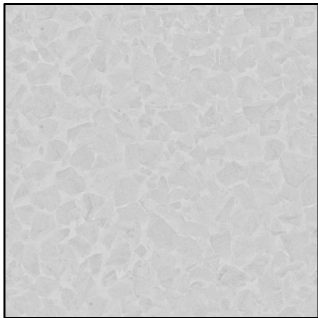
- **Texture**
- **Image Textures**
- **Procedural Textures**
- **Texture Mapping**

TEXTURE

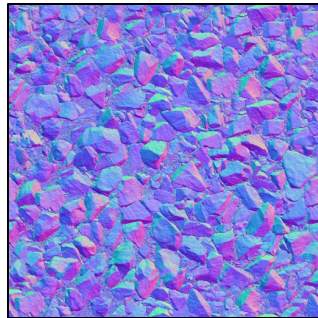
Texture

- **Textures modify the input for shading computations**
 - Either via (painted) images textures or procedural functions
- **Example texture maps for**
 - Reflectance, normals, shadows, reflections, essentially anything, ...

Roughness



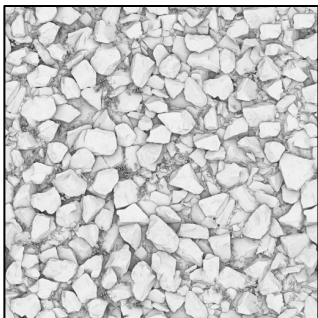
Normals



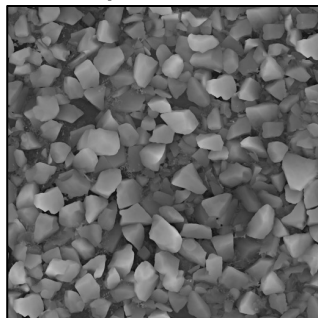
Albedo



Ambient Occlusion



Displacement



Polyhaven : <https://polyhaven.com/>

Texture

- Two BSDFs only, all the variations comes from textures



Definition: Textures

- **Textures map texture coordinates to shading values**
 - Input: 1D/2D/3D/4D texture coordinates
 - Explicitly given or derived via other data (e.g., position, direction, ...)
 - Output: Scalar or vector value
- **Modified values in shading computations**
 - Reflectance
 - Changes the diffuse or specular reflection coefficient (k_d, k_s)
 - Geometry and Normal (important for lighting)
 - Displacement mapping $P' = P + \Delta P$
 - Normal mapping $N' = N + \Delta N$
 - Bump mapping $N' = N(P + tN)$
 - Opacity
 - Modulating transparency (e.g., for fences in games)
 - Illumination
 - Light maps, environment mapping, reflection mapping
 - Anything else ...

IMAGE TEXTURES

Image Textures

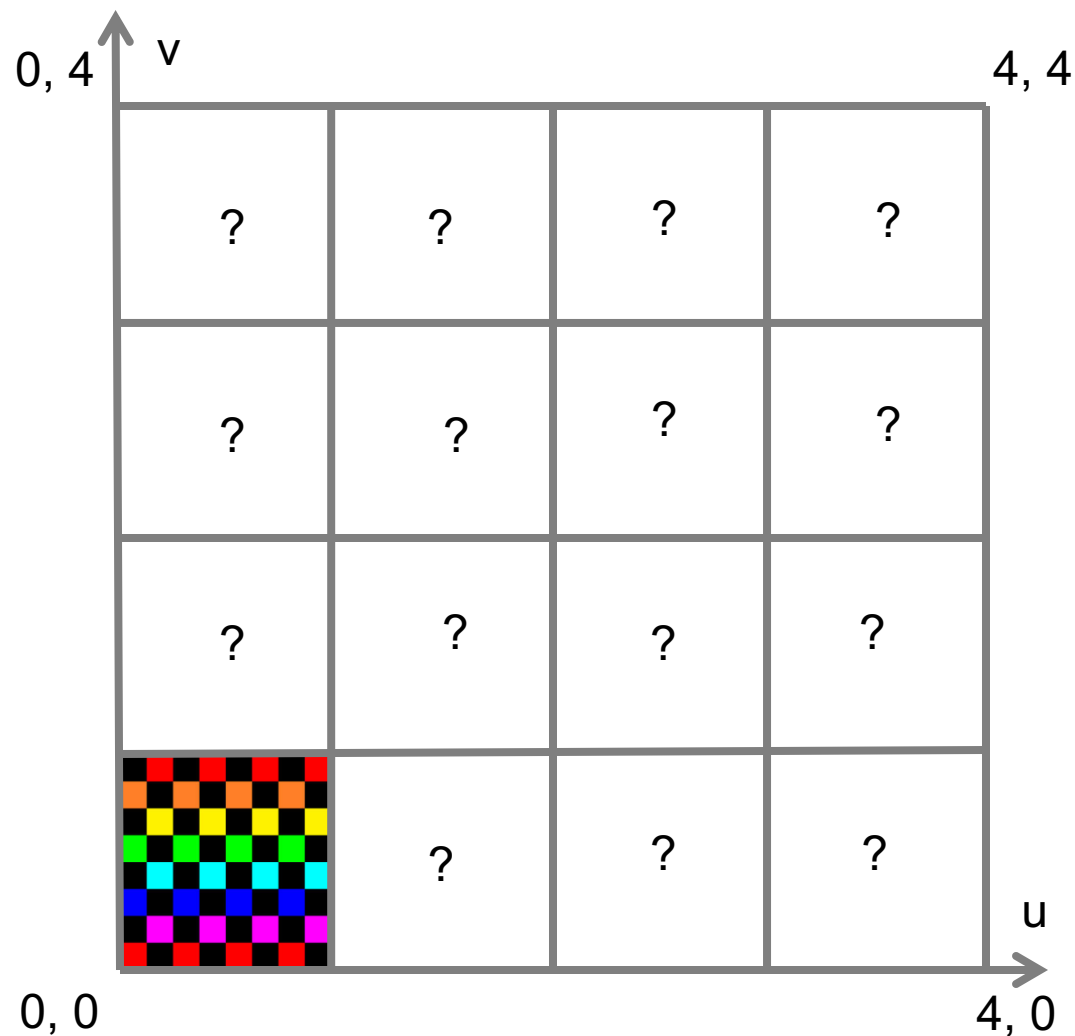
- **Image textures**

- Return the color of the image at a given point
- Point defined by mapping the texture coordinates $[0,1]^n$ to the entire image
- Images may be 1D (line of pixels), 2D, and 3D (stacks of images)
- Coordinates outside of $[0,1]^2$ can be mapped in different modes



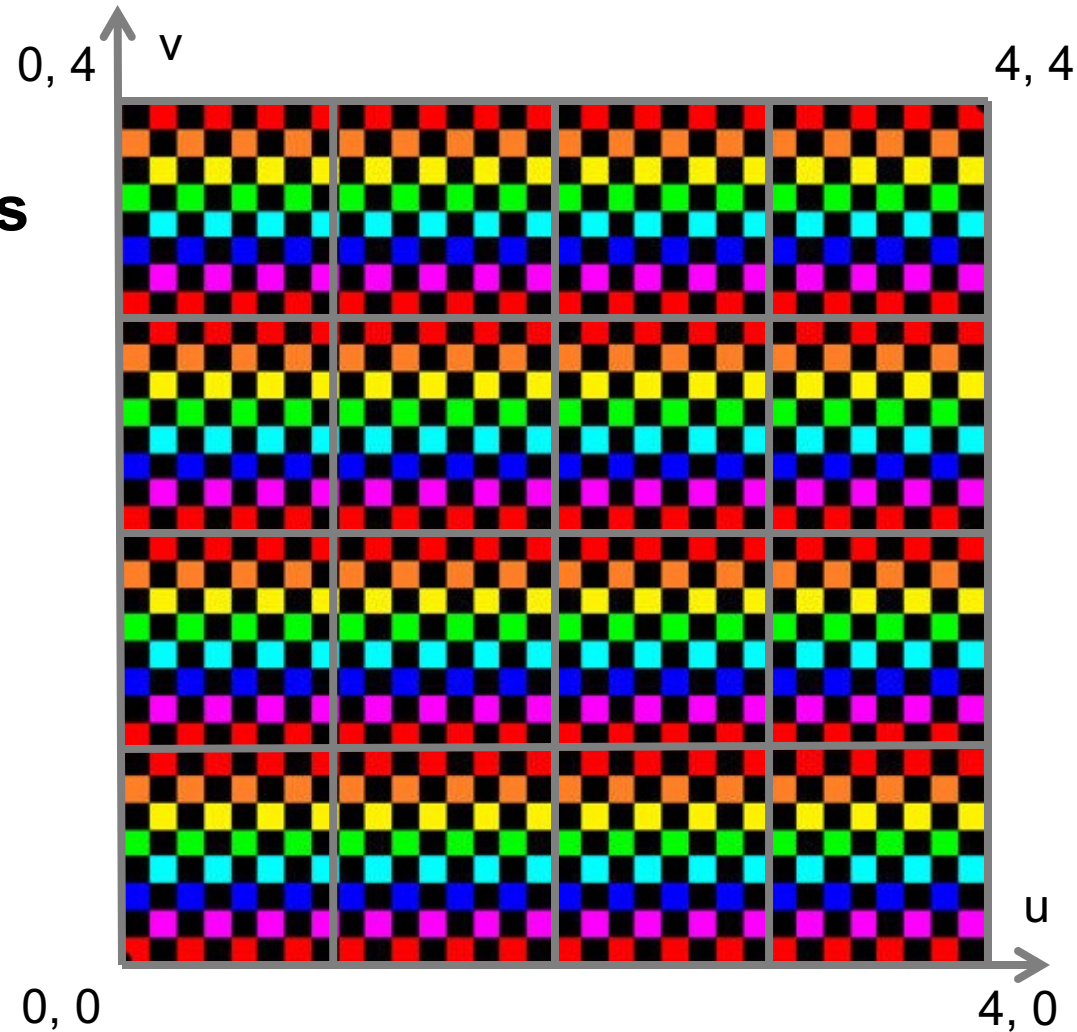
Wrap Mode

- **Texture Coordinates**
 - (u, v) in $[0, 1] \times [0, 1]$
- **What if?**
 - (u, v) not in unit square?



Wrap Mode

- Repeat
- Fractional Coordinates
 - $t_u = u - \lfloor u \rfloor$;
 - $t_v = v - \lfloor v \rfloor$;



Wrap Mode

- **Mirror**

- **Fractional Coordinates**

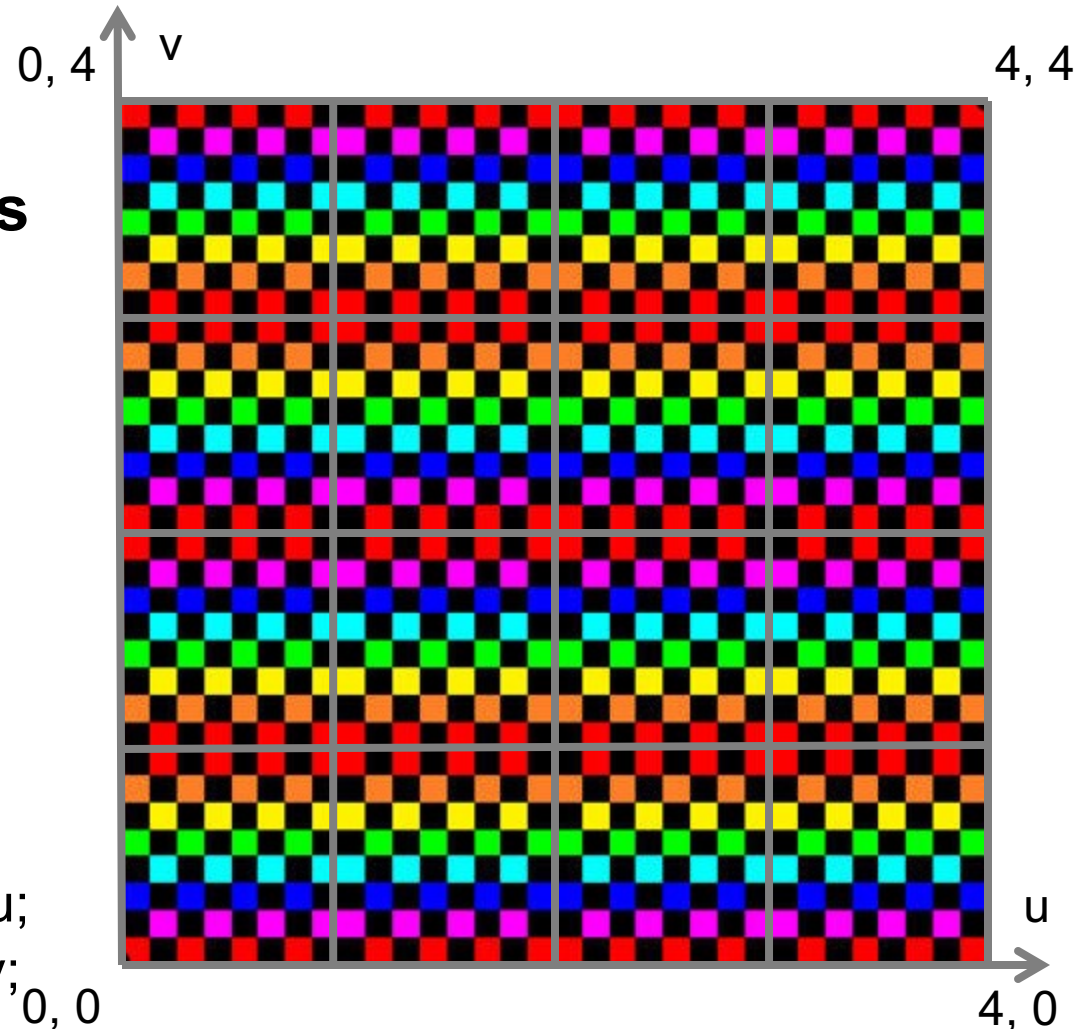
- $t_u = u - \lfloor u \rfloor$;
- $t_v = v - \lfloor v \rfloor$;

- **Lattice Coordinates**

- $l_u = \lfloor u \rfloor$;
- $l_v = \lfloor v \rfloor$;

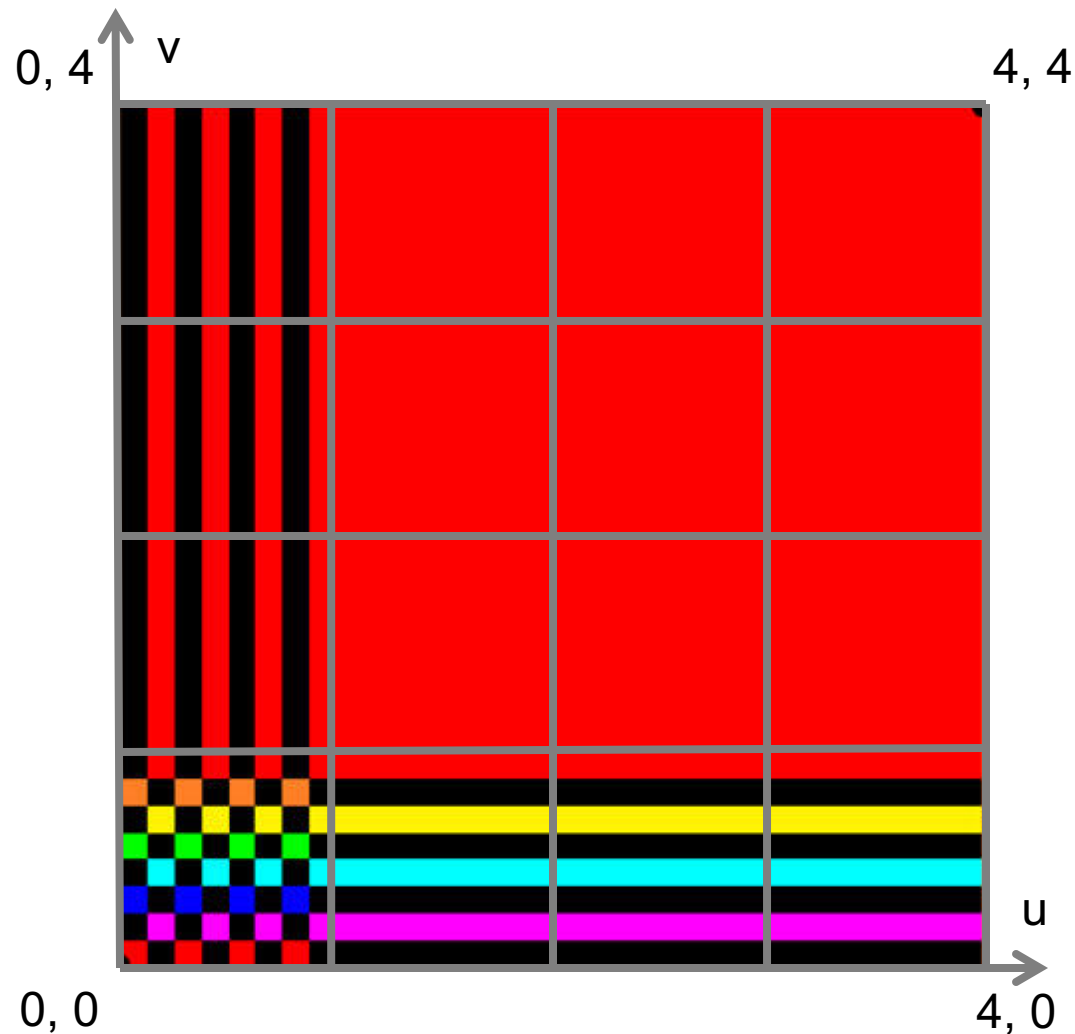
- **Mirror if Odd**

- if $(l_u \% 2 == 1)$ $t_u = 1 - t_u$;
- if $(l_v \% 2 == 1)$ $t_v = 1 - t_v$;



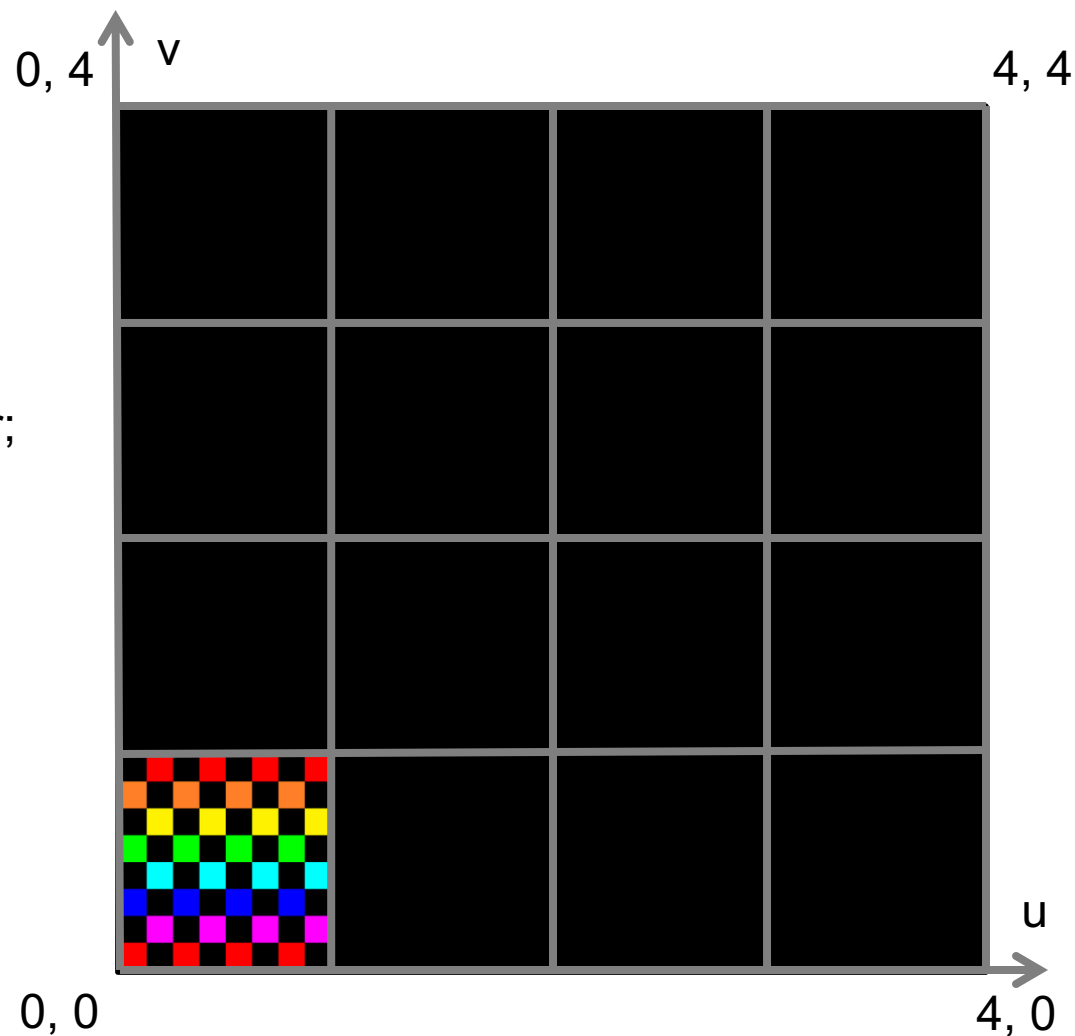
Wrap Mode

- **Clamp**
- **Clamp u to $[0, 1]$**
 - if $(u < 0)$ $tu = 0;$
 - else if $(u > 1)$ $tu = 1;$
 - else $tu = u;$
- **Clamp v to $[0, 1]$**
 - if $(v < 0)$ $tv = 0;$
 - else if $(v > 1)$ $tv = 1;$
 - else $tv = v;$



Wrap Mode

- **Border**
- **Check Bounds**
 - if ($u < 0 \parallel u > 1$
 - $\parallel v < 0 \parallel v > 1$)
 - return backgroundColor;
 - else
 - $tu = u;$
 - $tv = v;$



Wrap Mode

- **Comparison**



GL_REPEAT



GL_MIRRORED_REPEAT



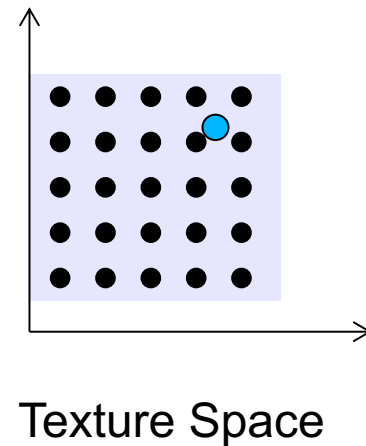
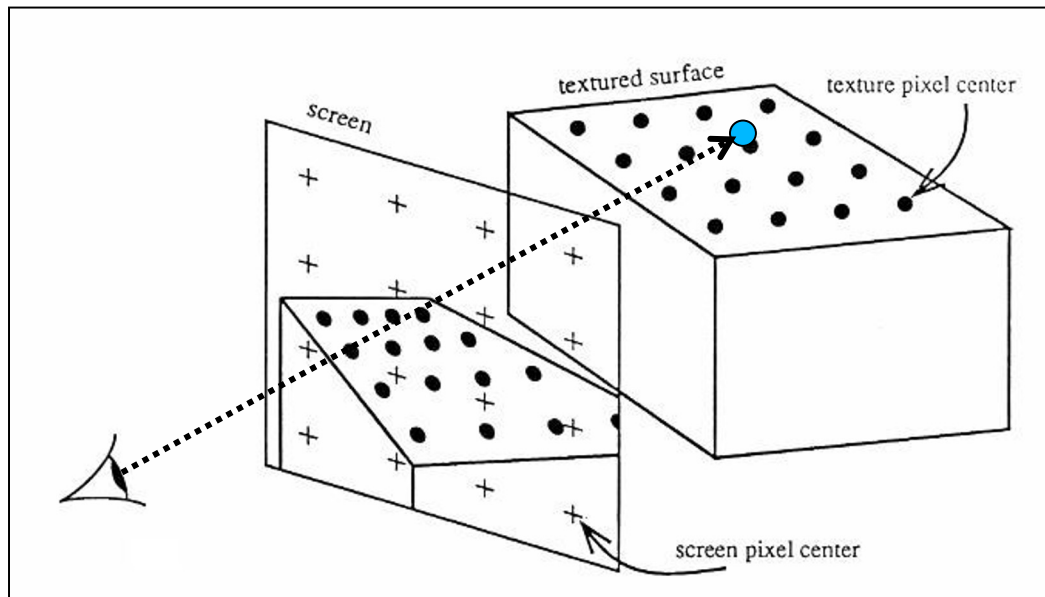
GL_CLAMP_TO_EDGE



GL_CLAMP_TO_BORDER

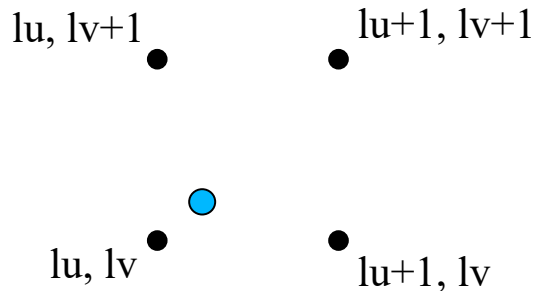
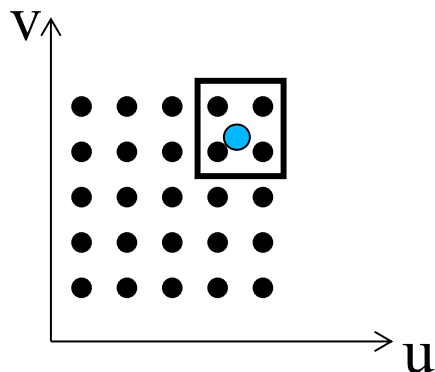
Reconstruction Filter

- **Image Texture**
 - Discrete set of sample values
- **In Practice**
 - Hit point generally does not exactly hit a texture sample
- **Reconstruct Continuous Function**
 - Use reconstruction filter to find color for hit point

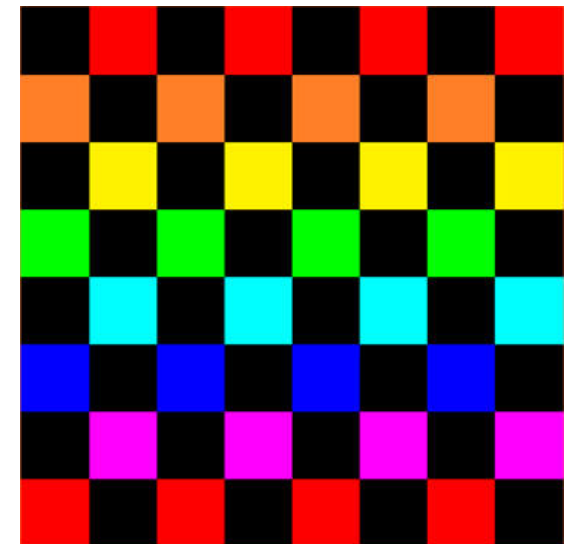
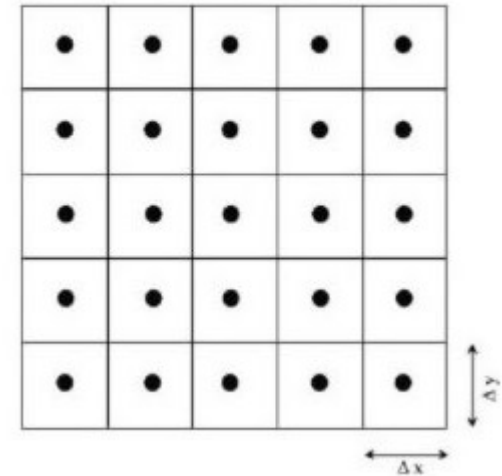


Nearest Neighbor

- **Local Coordinates**
 - Assuming cell-centered samples
 - $u = t_u * \text{resU}$;
 - $v = t_v * \text{resV}$;
- **Lattice Coordinates**
 - $l_u = \min(\lfloor u \rfloor, \text{resU} - 1)$;
 - $l_v = \min(\lfloor v \rfloor, \text{resV} - 1)$;
- **Texture Value**
 - return `image[lu, lv]`;

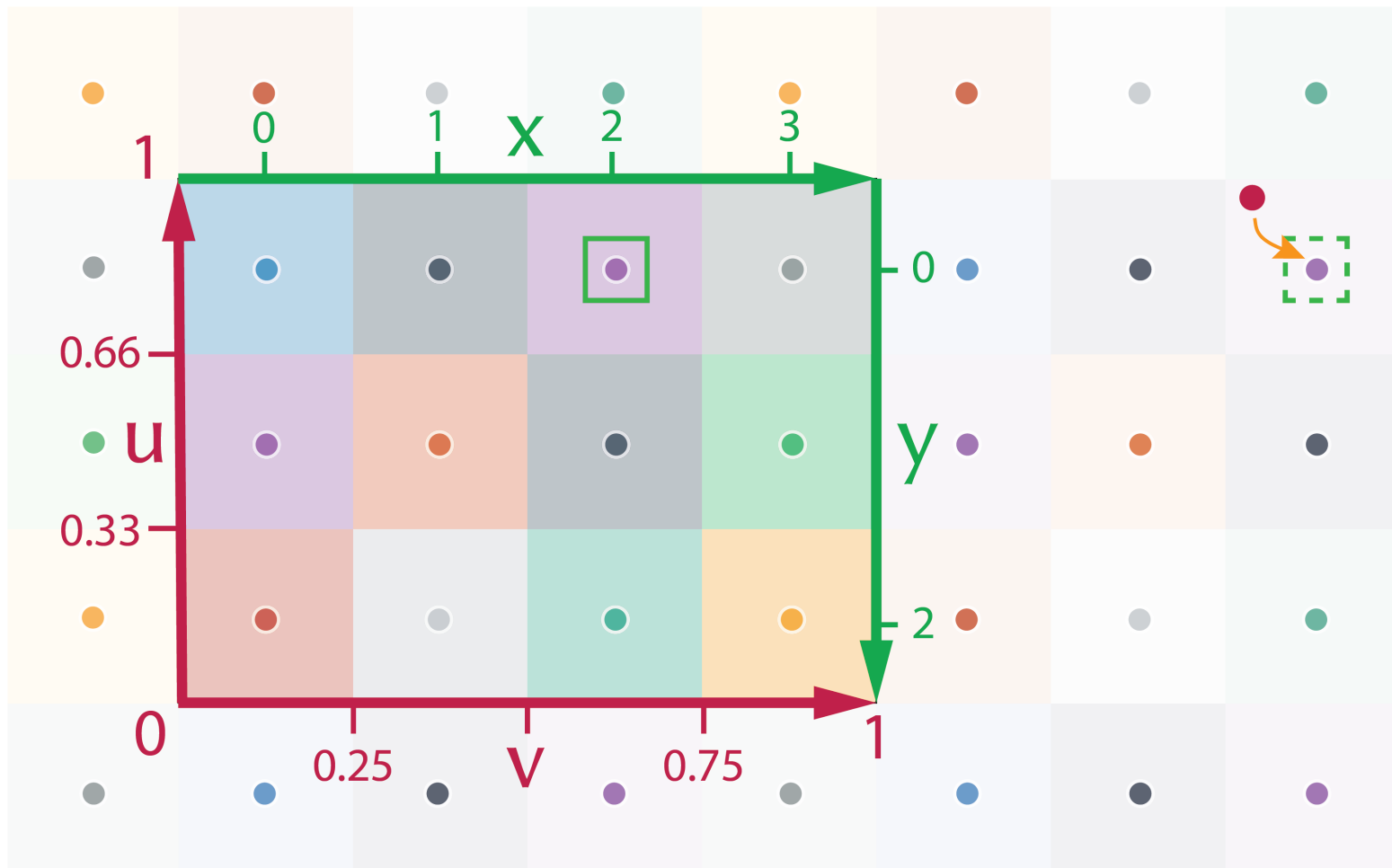


Pixel centred registration



Nearest Neighbor

- In Lightwave with Repeat Wrap Mode



Bilinear Interpolation

- **Local Coordinates**

- Assuming node-centered samples
- $u = t_u * (\text{resU} - 1);$
- $v = t_v * (\text{resV} - 1);$

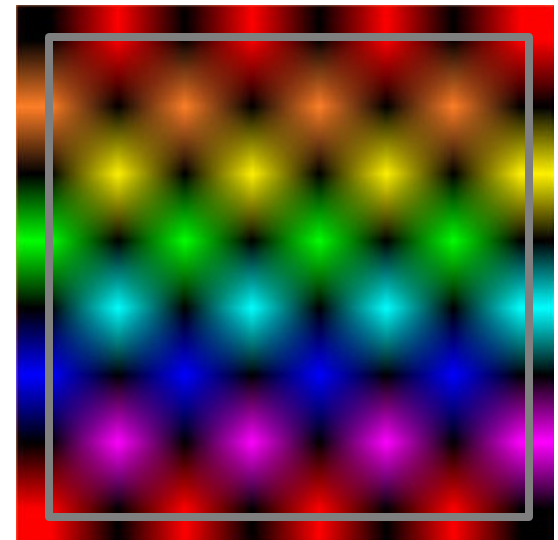
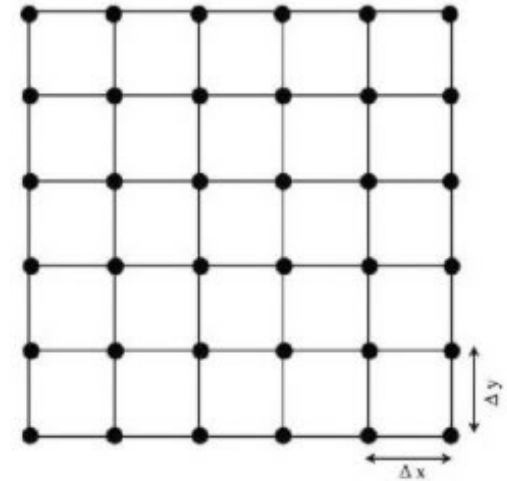
- **Fractional Coordinates**

- $f_u = u - \lfloor u \rfloor;$
- $f_v = v - \lfloor v \rfloor;$

- **Texture Value**

- $\text{return } (1-f_u) (1-f_v) \text{image}[\lfloor u \rfloor, \lfloor v \rfloor]$
+ $(1-f_u) (f_v) \text{image}[\lfloor u \rfloor, \lfloor v \rfloor + 1]$
+ $(f_u) (1-f_v) \text{image}[\lfloor u \rfloor + 1, \lfloor v \rfloor]$
+ $(f_u) (f_v) \text{image}[\lfloor u \rfloor + 1, \lfloor v \rfloor + 1]$

Grid node registration



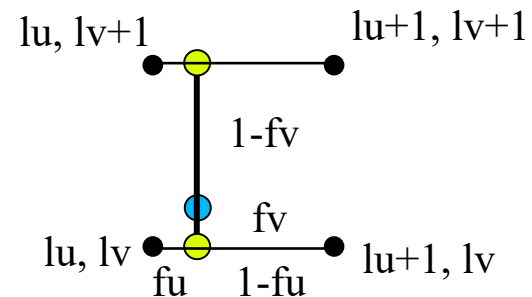
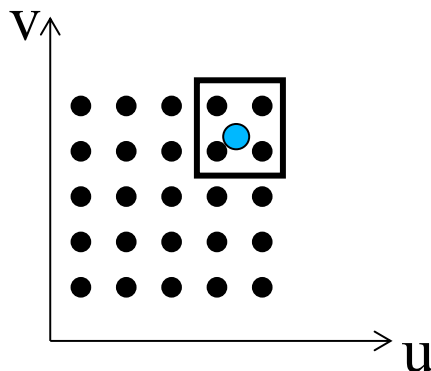
Bilinear Interpolation

- **Successive Linear Interpolations**

- $u0 = (1-fv) \text{ image}[\lfloor u \rfloor, \lfloor v \rfloor]$
+ $(fv) \text{ image}[\lfloor u \rfloor, \lfloor v \rfloor + 1];$

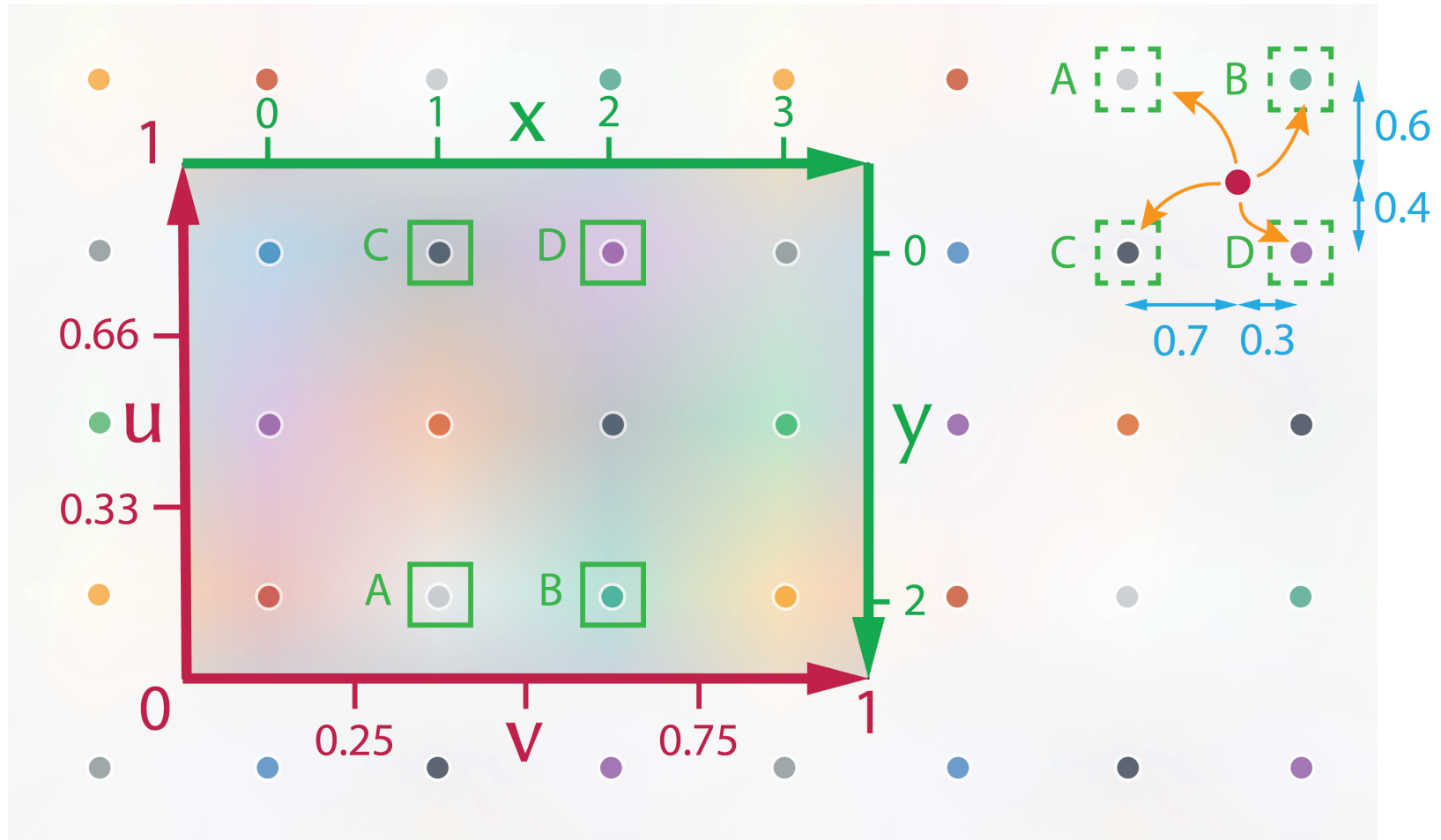
- $u1 = (1-fv) \text{ image}[\lfloor u \rfloor + 1, \lfloor v \rfloor]$
+ $(fv) \text{ image}[\lfloor u \rfloor + 1, \lfloor v \rfloor + 1];$

- return $(1-fu) u0$
+ $(fu) u1;$



Bilinear Interpolation

- In Lightwave with Repeat Wrap Mode



Nearest vs. Bilinear Interpolation



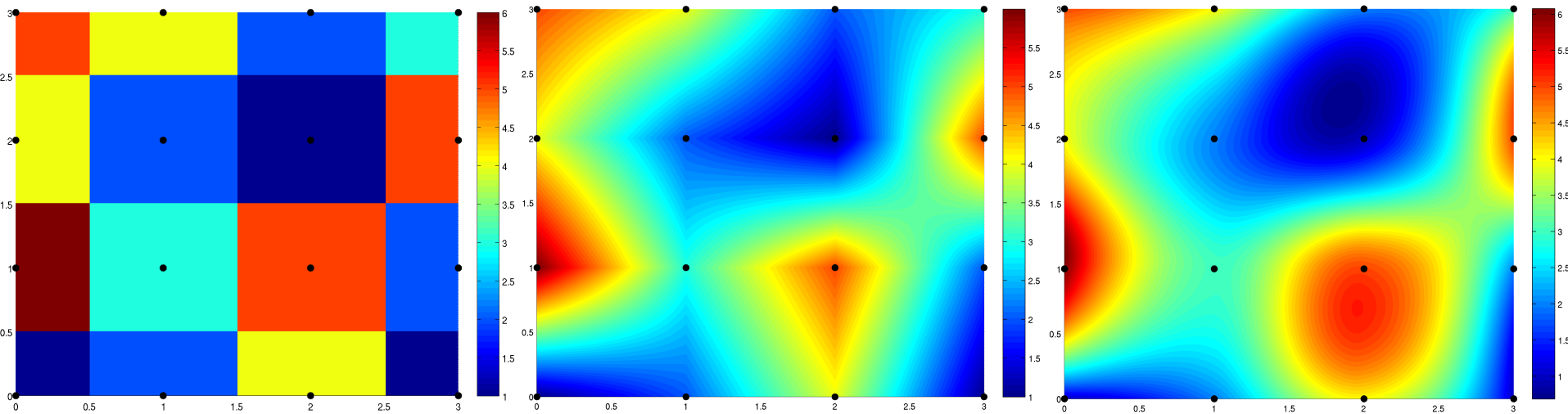
GL_NEAREST



GL_LINEAR

Bicubic Interpolation

- **Properties**
 - Assuming node-centered samples
 - Essentially based on cubic splines (see later)
- **Pros**
 - Even smoother
- **Cons**
 - More complex & expensive (4x4 kernel)
 - Overshoot



Discussion: Image Textures

- **Pros**

- Simple generation
 - Painted, simulation, ...
- Simple acquisition
 - Photos, videos

- **Cons**

- Illumination “frozen” during acquisition (e.g. photo)
- Limited resolution
- Susceptible to aliasing
- High memory requirements (often HUGE for films, 100s of GB)
- Issues when mapping 2D image onto 3D object

PROCEDURAL TEXTURES

Discussion

- **Cons**

- Possibly non-trivial programming

- **Pros**

- Flexibility & parametric control
- Unlimited resolution
- Anti-aliasing possible
- Low memory requirements
- May be directly defined as 3D “image” mapped to 3D geometry
- Low-cost visual complexity

2D Checkerboard

- **Lattice Coordinates**

- $|u| = \lfloor u \rfloor$

- $|v| = \lfloor v \rfloor$

- **Compute Parity**

- $\text{parity} = (|u| + |v|) \% 2;$

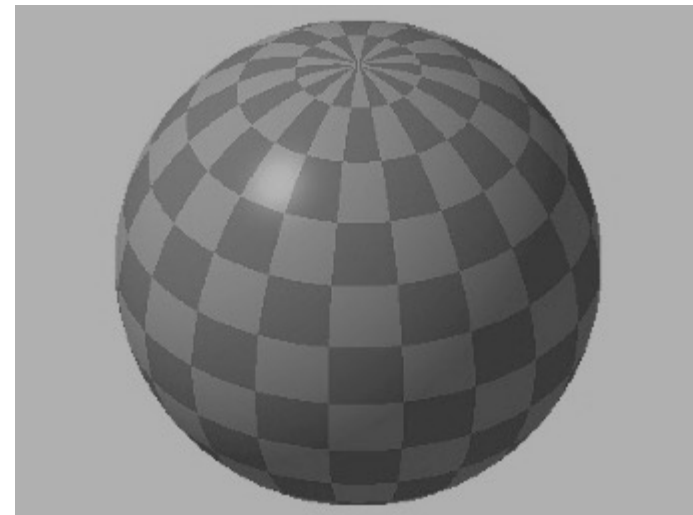
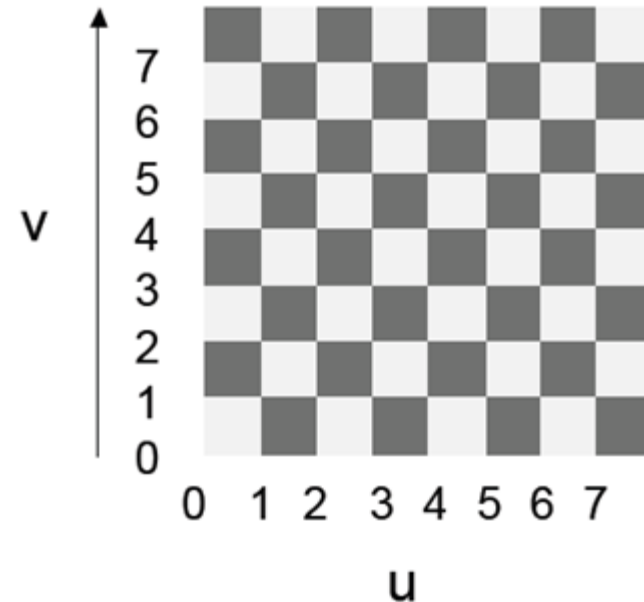
- **Return Color**

- if ($\text{parity} == 1$)

- return color1;

- else

- return color0;



3D Checkerboard - Solid Texture

- **Lattice Coordinates**

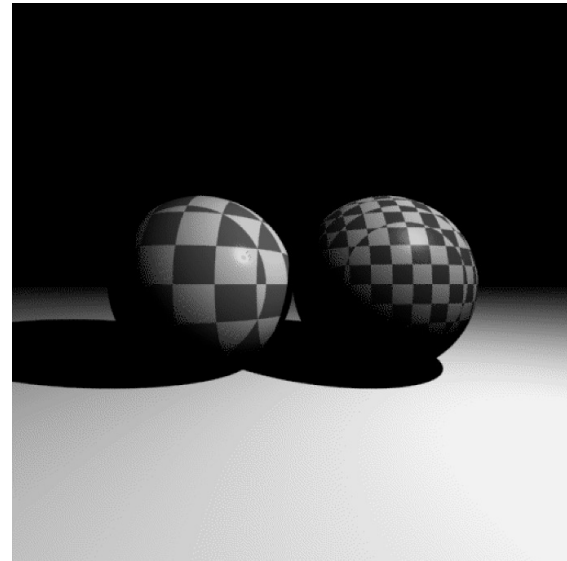
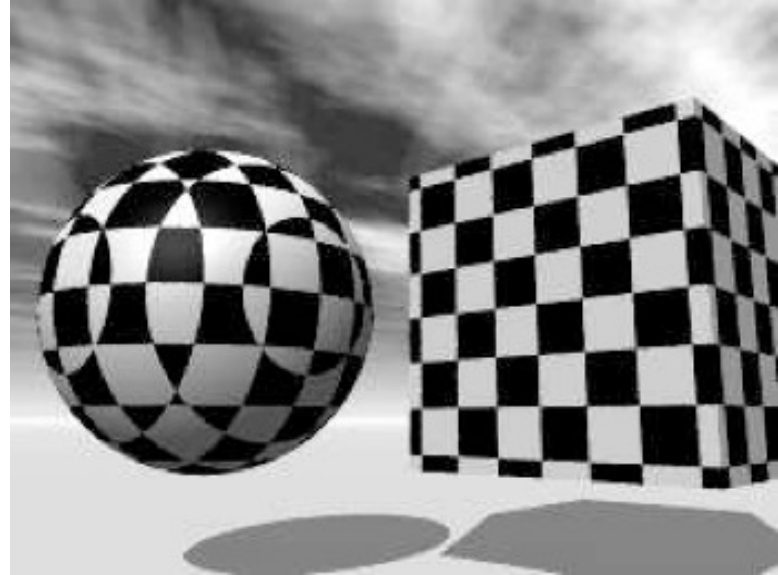
- $lu = \lfloor u \rfloor$
- $lv = \lfloor v \rfloor$
- $lw = \lfloor w \rfloor$

- **Compute Parity**

- $parity = (lu + lv + lw) \% 2;$

- **Return Color**

- if ($parity == 1$)
 - return color1;
- else
 - return color0;



2D Checkerboard – Nearest-Node

- **Fractional Coordinates**

- $f_u = u - \lfloor u \rfloor$

- $f_v = v - \lfloor v \rfloor$

- **Compute Booleans**

- $b_u = f_u < 1/2$;

- $b_v = f_v < 1/2$;

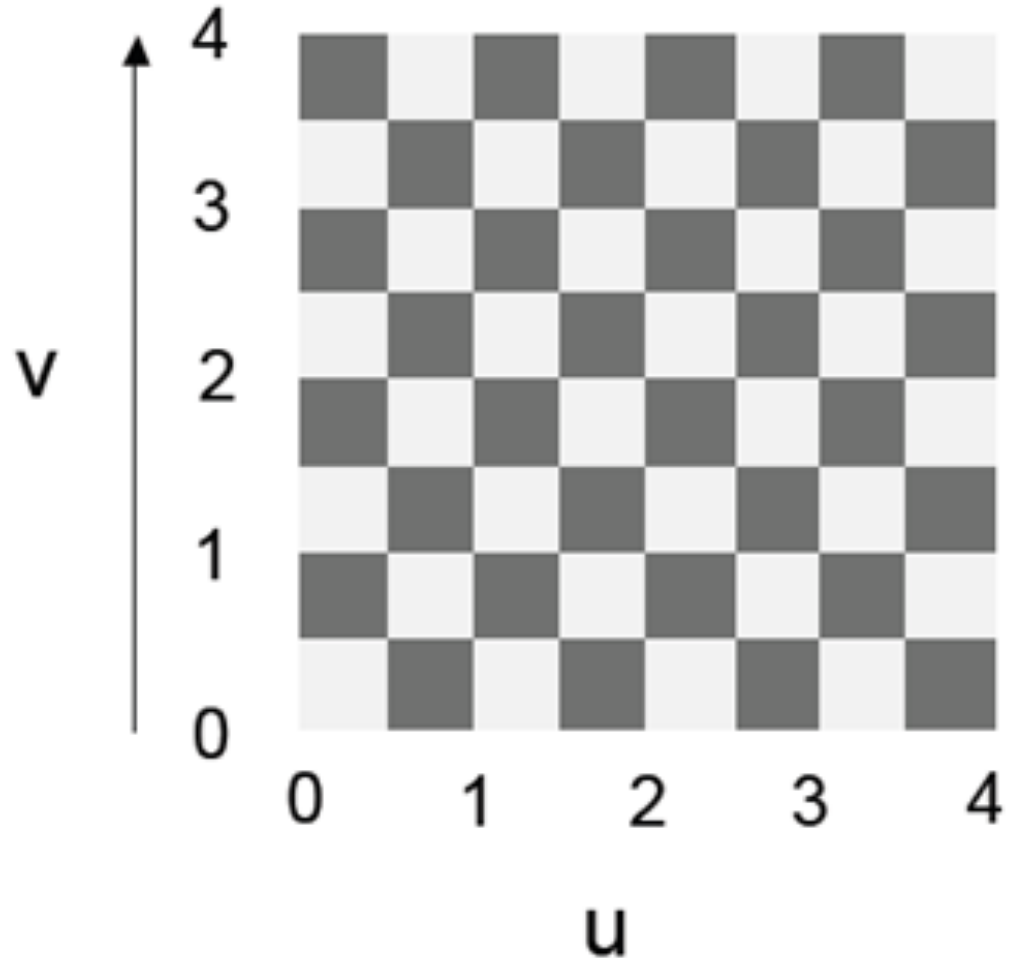
- **Return Color**

- if ($b_u \wedge b_v$)

- return color1;

- else

- return color0;



Tile

- **Fractional Coordinates**

- $f_u = u - \lfloor u \rfloor$

- $f_v = v - \lfloor v \rfloor$

- **Compute Booleans**

- $b_u = f_u < \text{groutWidth};$

- $b_v = f_v < \text{groutWidth};$

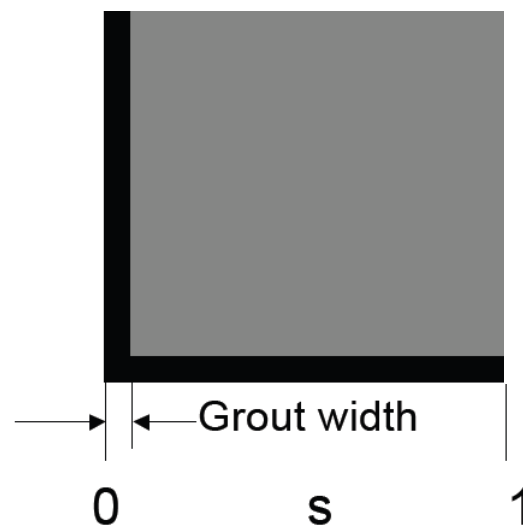
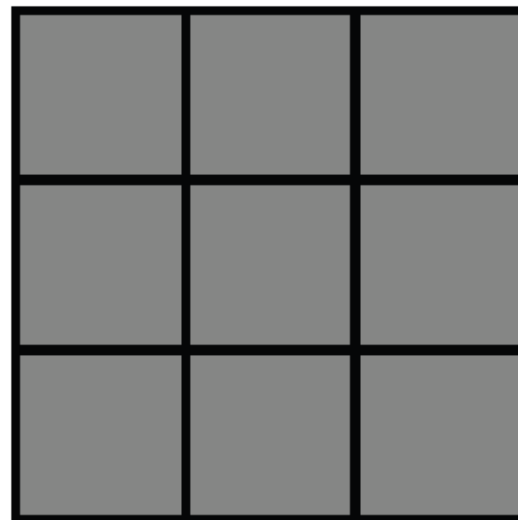
- **Return Color**

- if ($b_u \parallel b_v$)

- return groutColor;

- else

- return tileColor;



Brick

- **Shift Column for Odd Rows**

- $\text{parity} = \lfloor v \rfloor \% 2;$
- $u -= \text{parity} * 0.5;$

- **Fractional Coordinates**

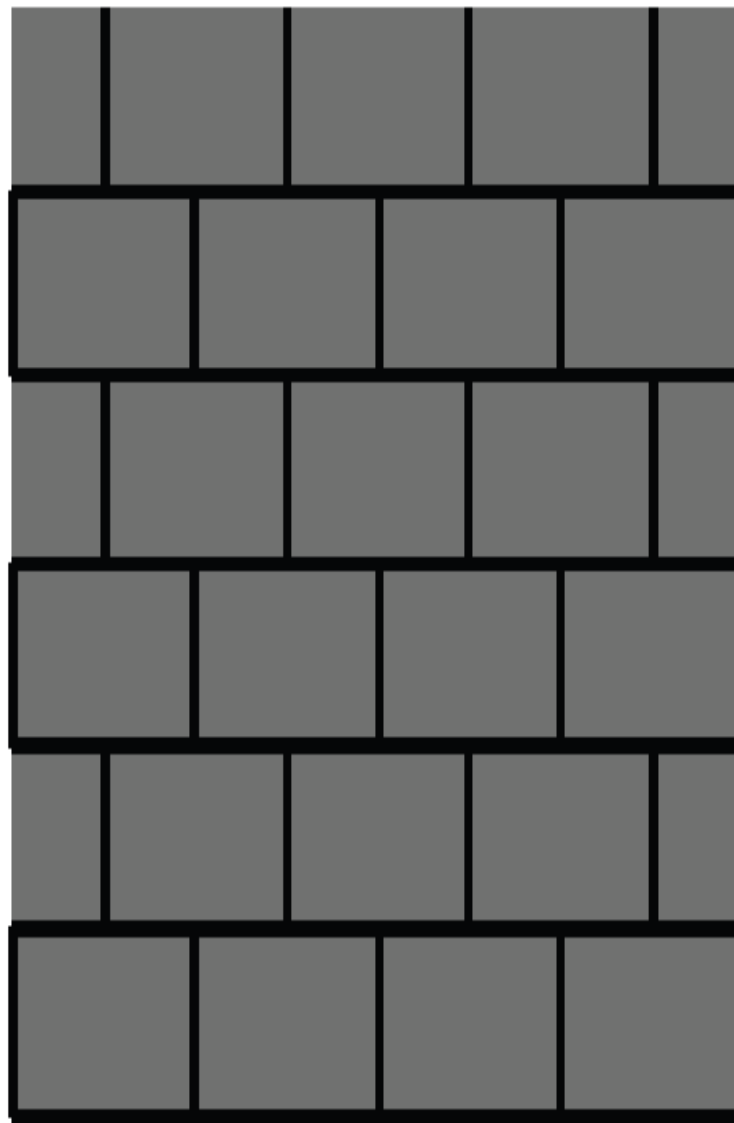
- $f_u = u - \lfloor u \rfloor$
- $f_v = v - \lfloor v \rfloor$

- **Compute Booleans**

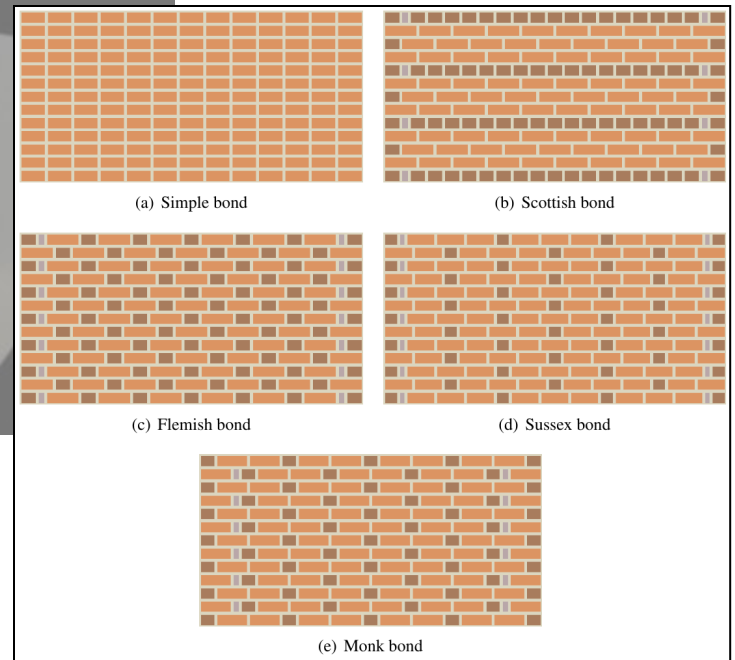
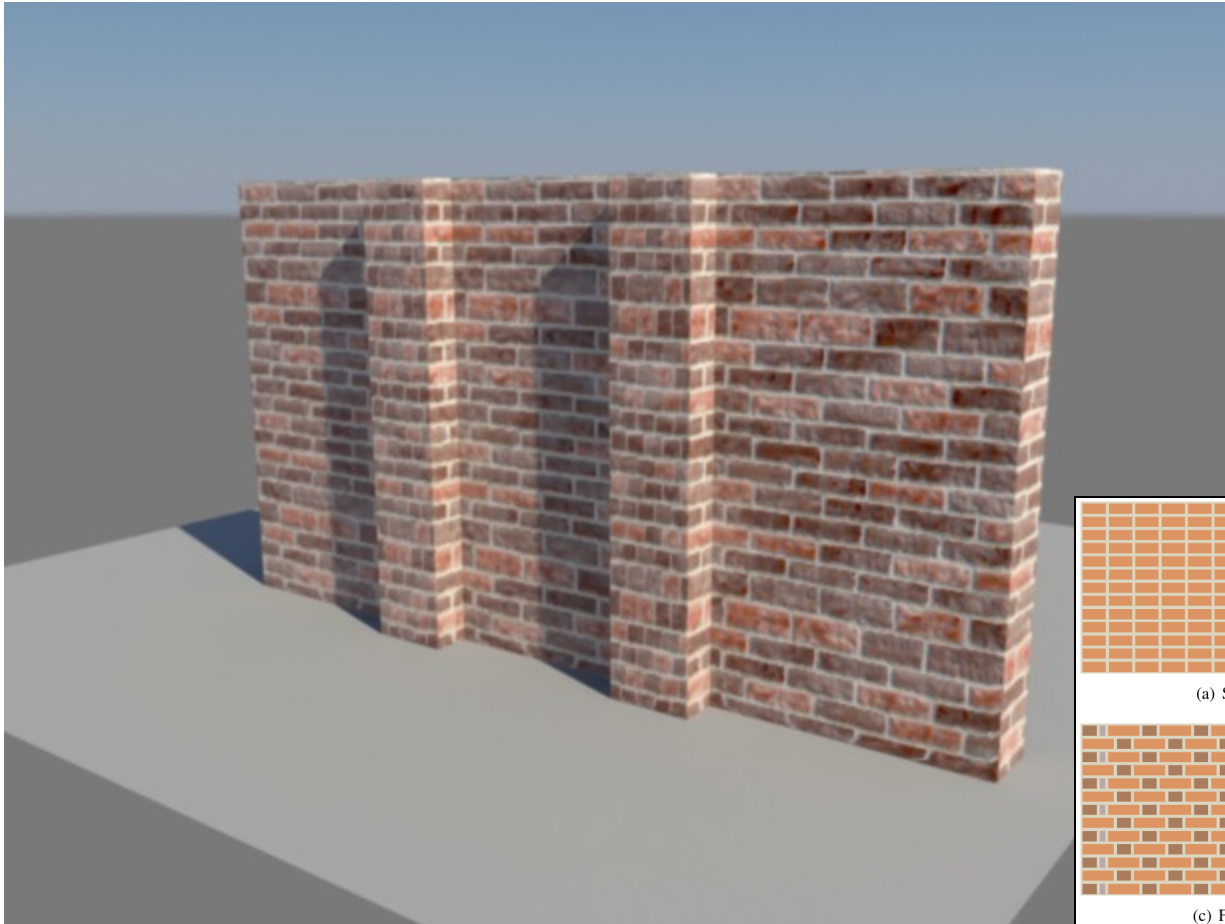
- $bu = f_u < \text{mortarWidth};$
- $bv = f_v < \text{mortarWidth};$

- **Return Color**

- if ($bu \parallel bv$)
 - return mortarColor;
- else
 - return brickColor;

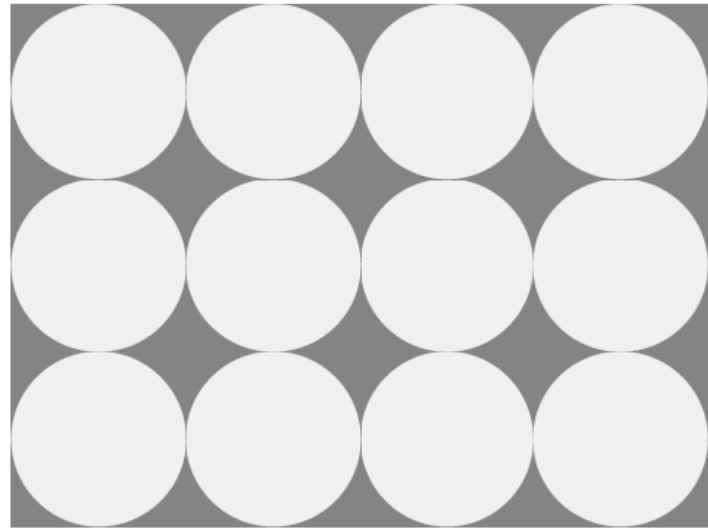


More Variation

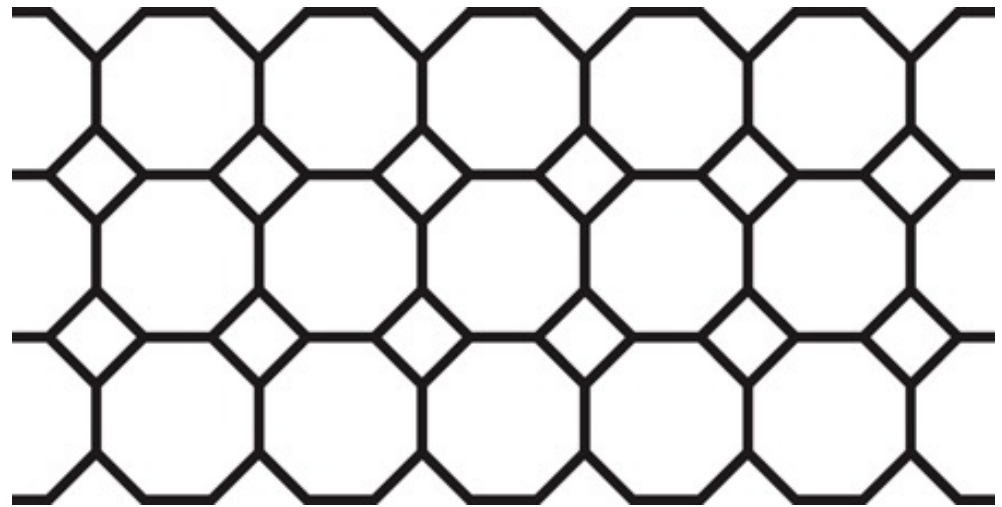


Other Patterns

- **Circular Tiles**



- **Octagonal Tiles**



- **Use your imagination!**

Perlin Noise

- **Natural Patterns**

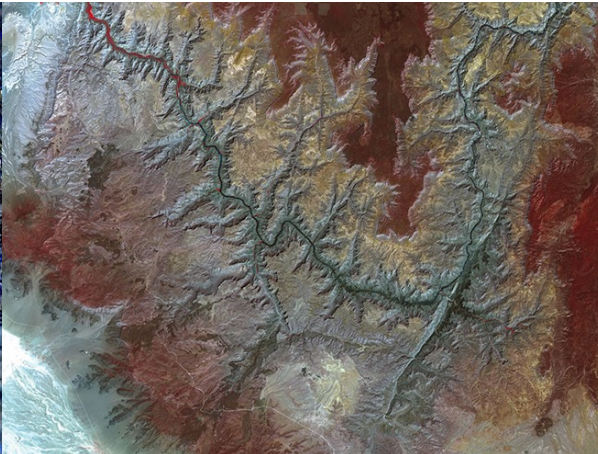
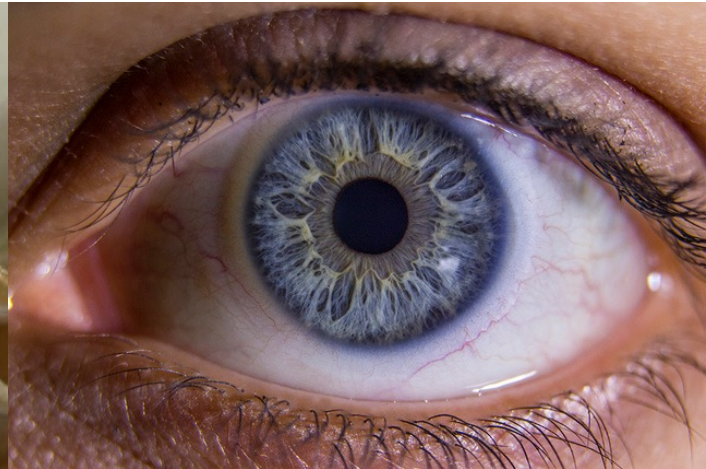
- Similarity between patches at different locations
 - Repetitiveness, coherence (e.g. skin of a tiger or zebra)
- Similarity on different resolution scales
 - Self-similarity
- But never completely identical
 - Additional disturbances, turbulence, noise

- **Mimic Statistical Properties**

- Purely empirical approach
- Looks convincing, but has nothing to do with material's physics

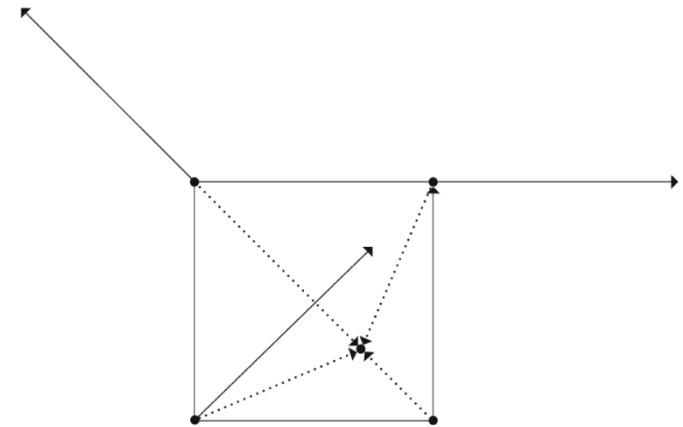
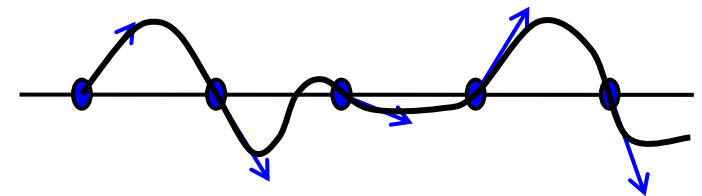
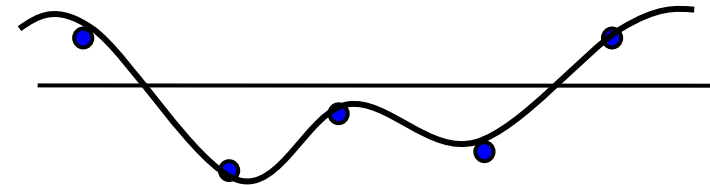
Perlin Noise

- **Natural Fractals**



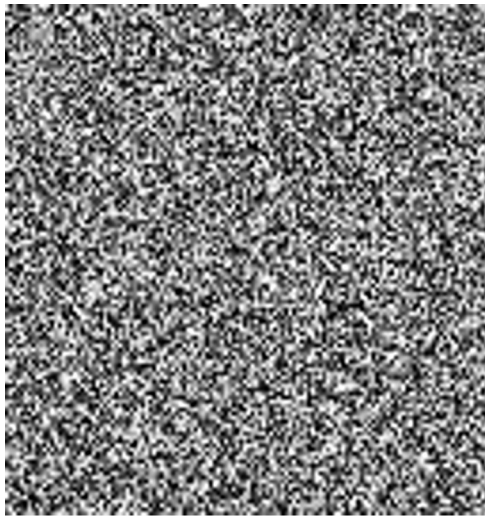
Noise Function

- **Noise(x, y, z)**
 - Statistical invariance under rotation
 - Statistical invariance under translation
 - Roughly fixed frequency of ~ 1 Hz
- **Integer Lattice (i, j, k)**
 - Value noise
 - Random value at lattice points
 - Gradient noise
 - Random gradient vector at lattice point
 - Compute lattice values as dot products
 - Interpolation
 - Bi-/tri-linear or cubic (Hermite spline)
 - Hash function
 - Randomized look up
 - Virtually infinite extent

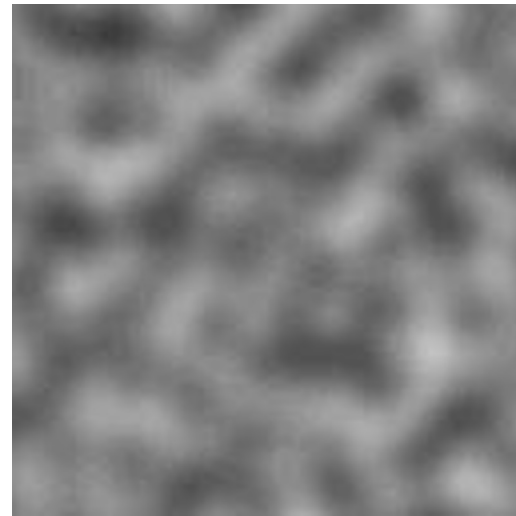


Noise vs. Noise

- **Value Noise vs. Gradient Noise**
 - Gradient noise has lower regularity artifacts
 - More high frequencies in noise spectrum
- **Random Values vs. Perlin Noise**
 - Stochastic vs. deterministic



Random values
at each pixel



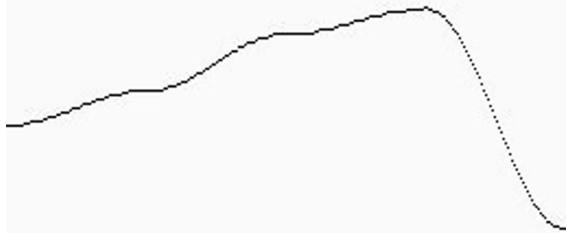
Gradient noise

Turbulence Function

- **Noise Function**
 - Single spike in frequency spectrum
- **Natural Textures**
 - Decreasing amplitude for high frequencies
- **Turbulence from Noise**
 - $Turbulence(x) = \sum_{i=0}^k |a_i * noise(f_i x)|$
 - Frequency: $f_i = 2^i$
 - Amplitude: $a_i = 1 / p^i$
 - Persistence: p typically $p=2$
 - Power spectrum : $a_i = 1 / f_i$
 - Brownian motion: $a_i = 1 / f_i^2$
 - Summation truncation
 - 1st term: noise(x)
 - 2nd term: noise(2x)/2
 - ...
 - Until period $(1/f_k) < 2$ pixel-size (band limit)

Synthesis of Turbulence (1-D)

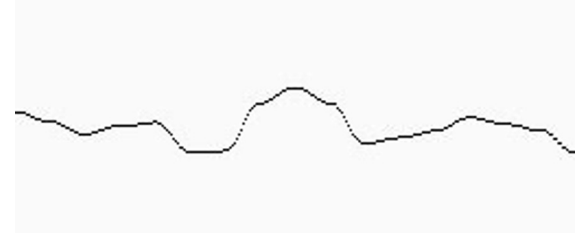
Amplitude : 128
frequency : 4



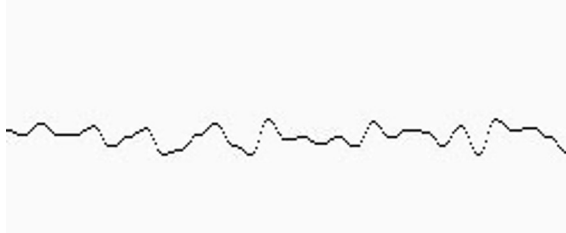
Amplitude : 64
frequency : 8



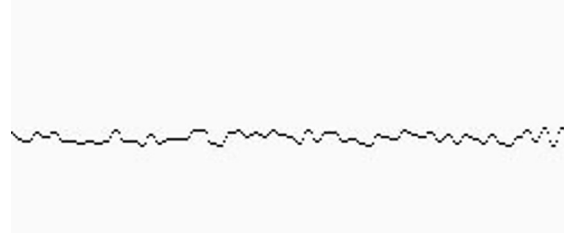
Amplitude : 32
frequency : 16



Amplitude : 16
frequency : 32



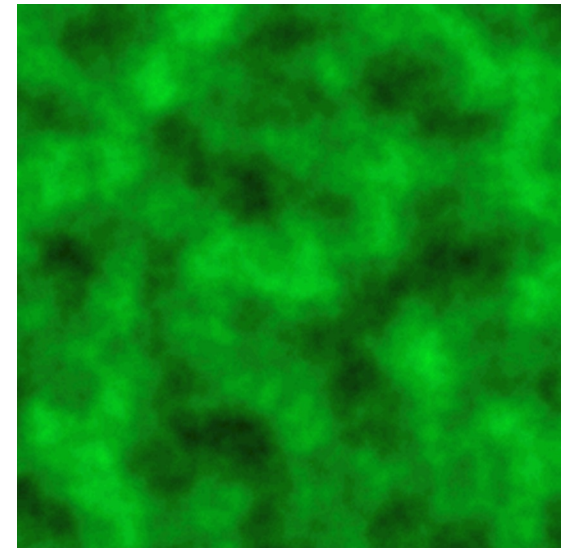
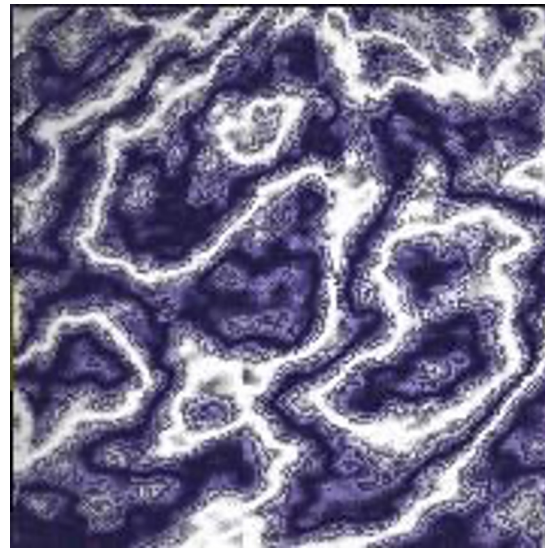
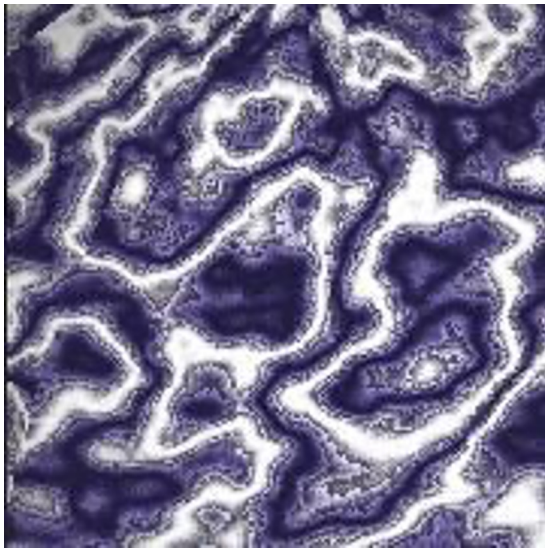
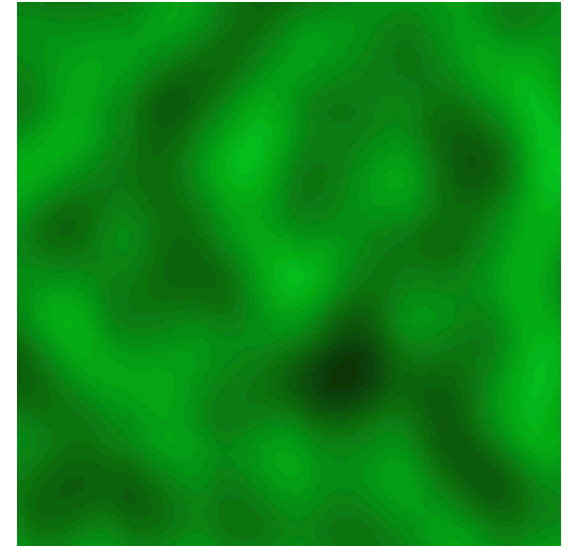
Amplitude : 8
frequency : 64



Sum of Noise Functions = (Perlin Noise)



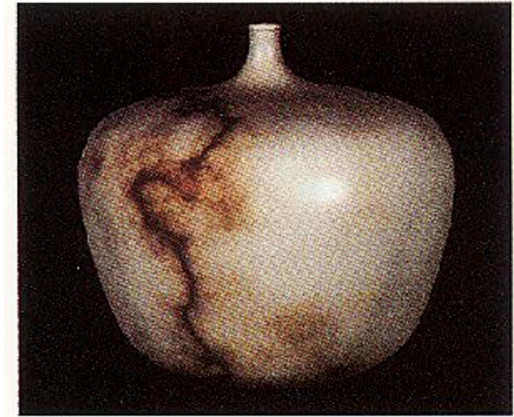
Synthesis of Turbulence (2-D)



Example: Marble

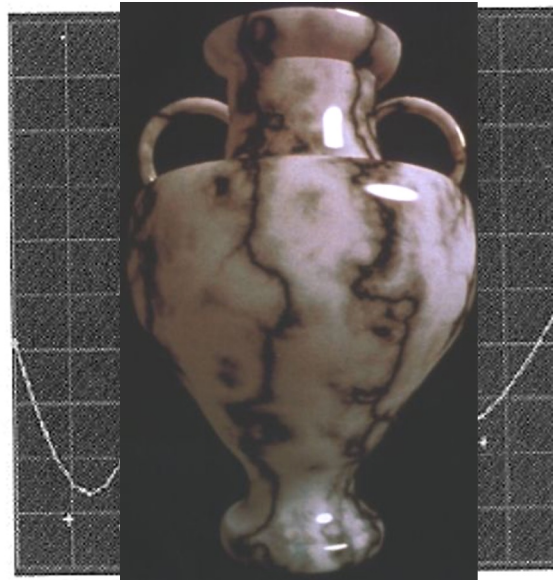
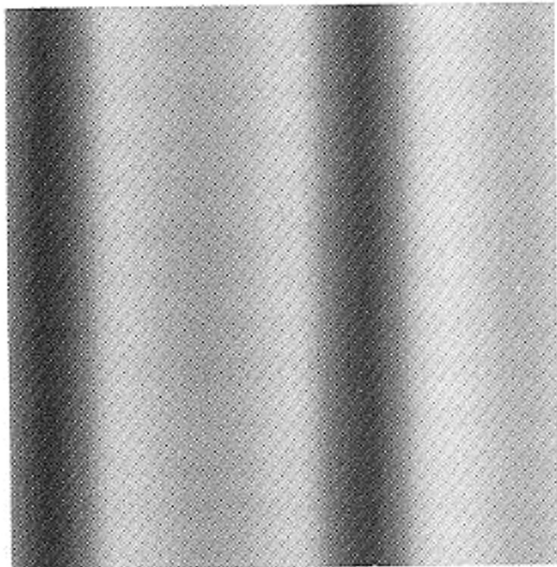
- **Overall Structure**

- Alternating layers of white and colored marble
- $f_{\text{marble}}(x,y,z) := \text{marble_color}(\sin(x))$
- `marble_color` : transfer function (see lower left)



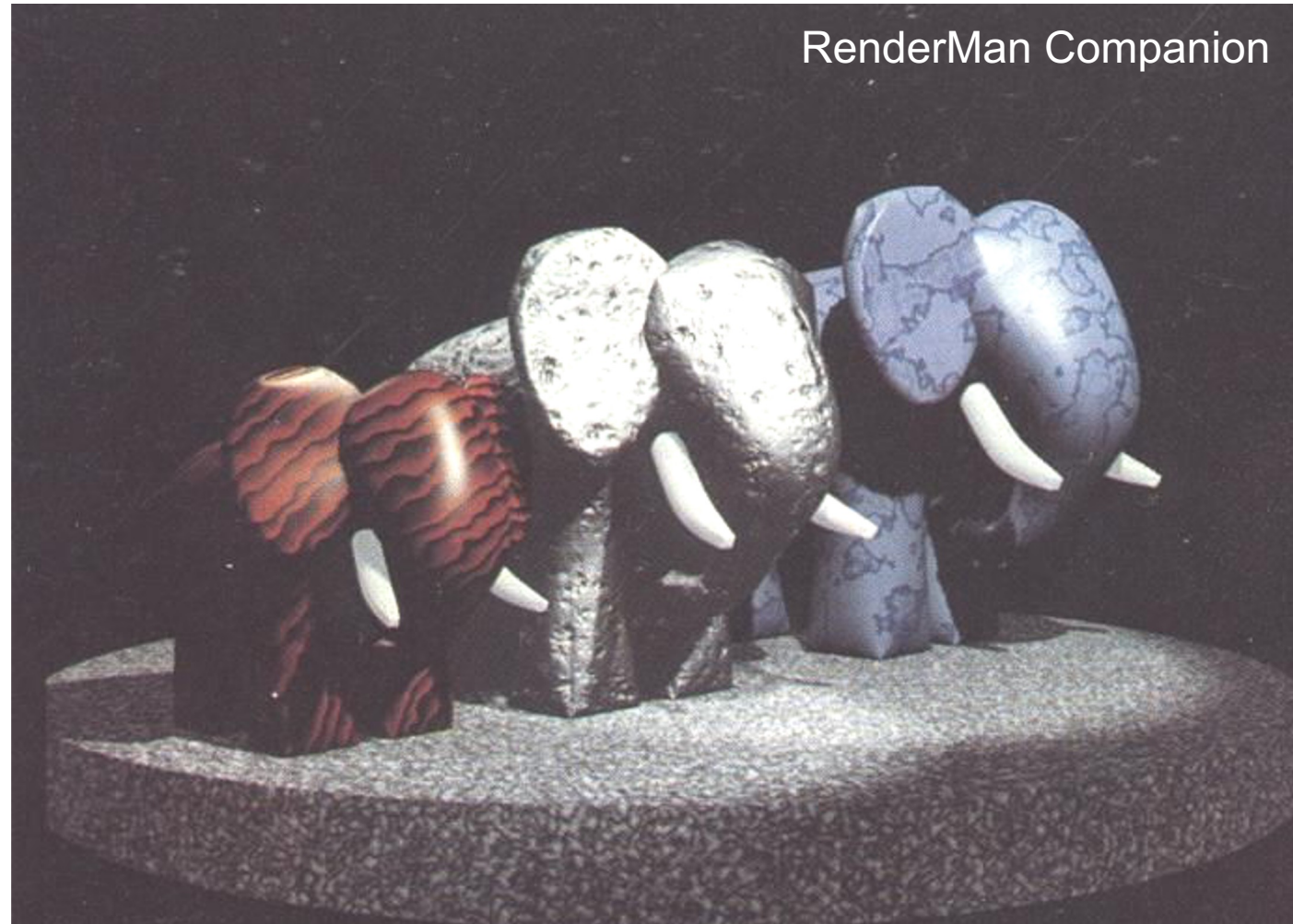
- **Realistic Appearance**

- Simulated turbulence
- $f_{\text{marble}}(x,y,z) := \text{marble_color}(\sin(x + \text{turbulence}(x, y, z)))$



Solid Noise

- **3D Noise Texture**
 - Wood
 - Bump map
 - Marble



Others Applications

- **Bark**
 - Turbulated saw-tooth function
- **Clouds**
 - White blobs
 - Turbulated transparency along edge
- **Animation**
 - Vary procedural texture function's parameters over time
- **See [Rainforest ShaderToy](#)**

TEXTURE MAPPING

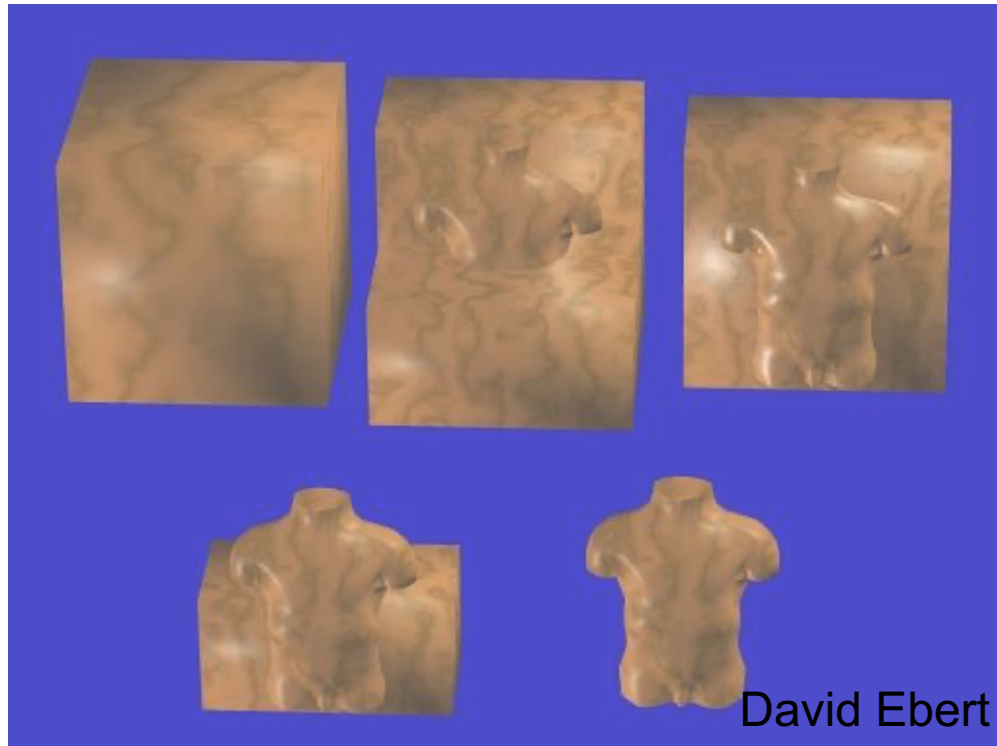
Textures Coordinates

- **Solid Textures**

- 3D world/object (x,y,z) coords \rightarrow 3D (u,v,w) texture coordinates
- Similar to carving object out of material block

- **2D Textures**

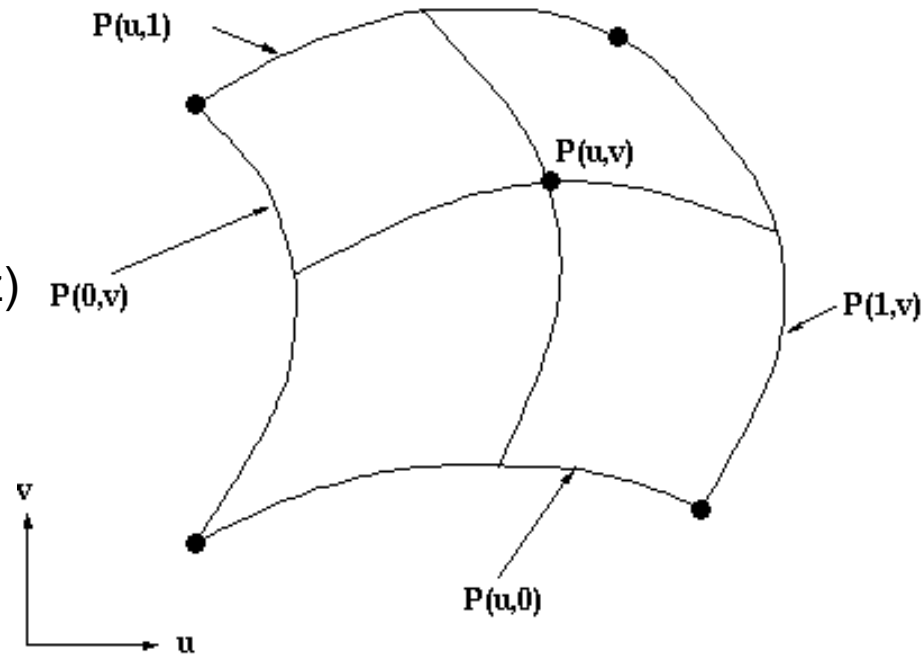
- 3D Cartesian (x,y,z) coordinates \rightarrow 2D (u,v) texture coordinates?



Parametric Surfaces

- **Definition**

- Surface defined by parametric function
 - $(x, y, z) = p(u, v)$
- Input
 - Parametric coordinates: (u, v)
- Output
 - Cartesian coordinates: (x, y, z)



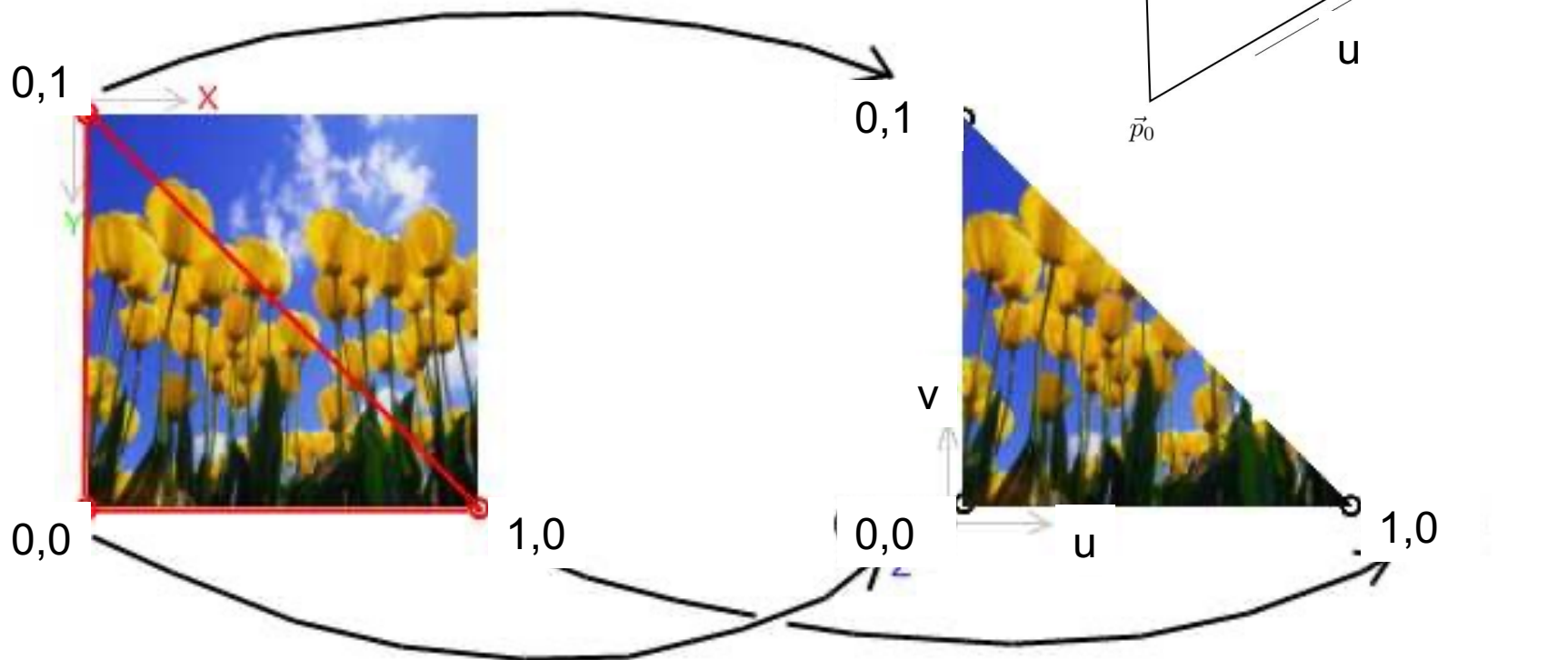
- **Texture Coordinates**

- Directly derived from surface parameterization
- Invert parametric function
 - From world coordinates to parametric coordinates

Parametric Surfaces

- **Triangle**

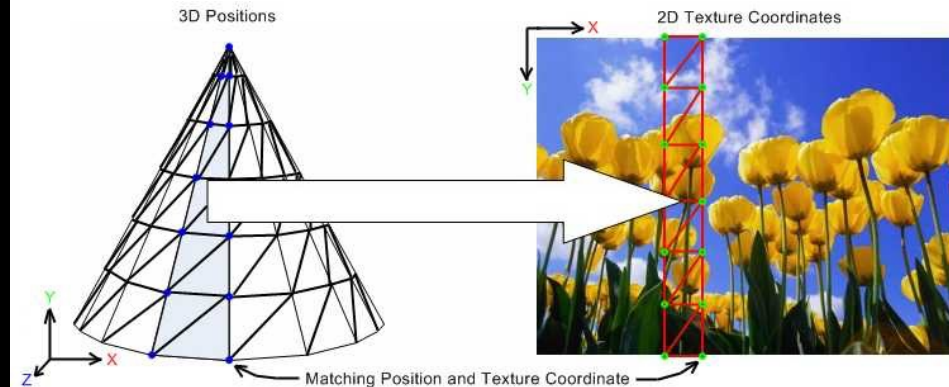
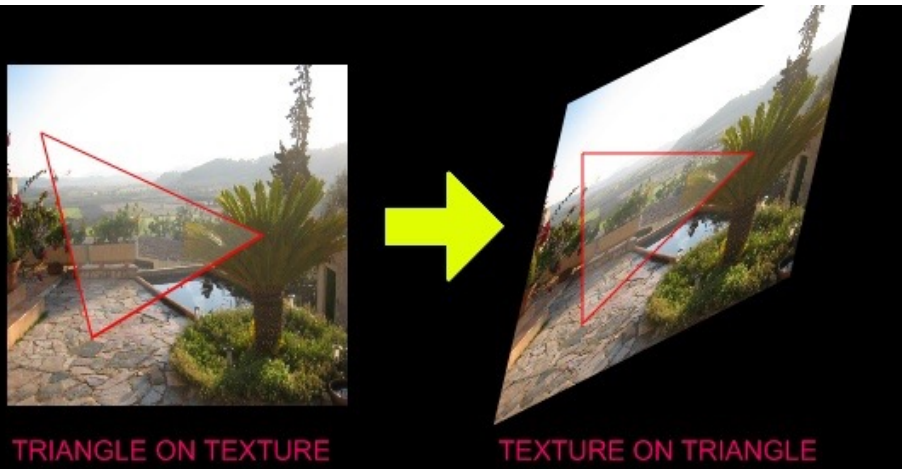
- Use barycentric coordinates directly
- $p(u, v) = (1 - u - v)p_0 + up_1 + vp_2$



Parametric Surfaces

- **Triangle Mesh**

- Associate a predefined texture coordinate to each triangle vertex
 - Interpolate texture coordinates using barycentric coordinates
 - $u = \lambda_0 p_{0u} + \lambda_1 p_{1u} + \lambda_2 p_{2u}$
 - $v = \lambda_0 p_{0v} + \lambda_1 p_{1v} + \lambda_2 p_{2v}$
- Texture mapped onto manifold
 - Single texture shared by many triangles



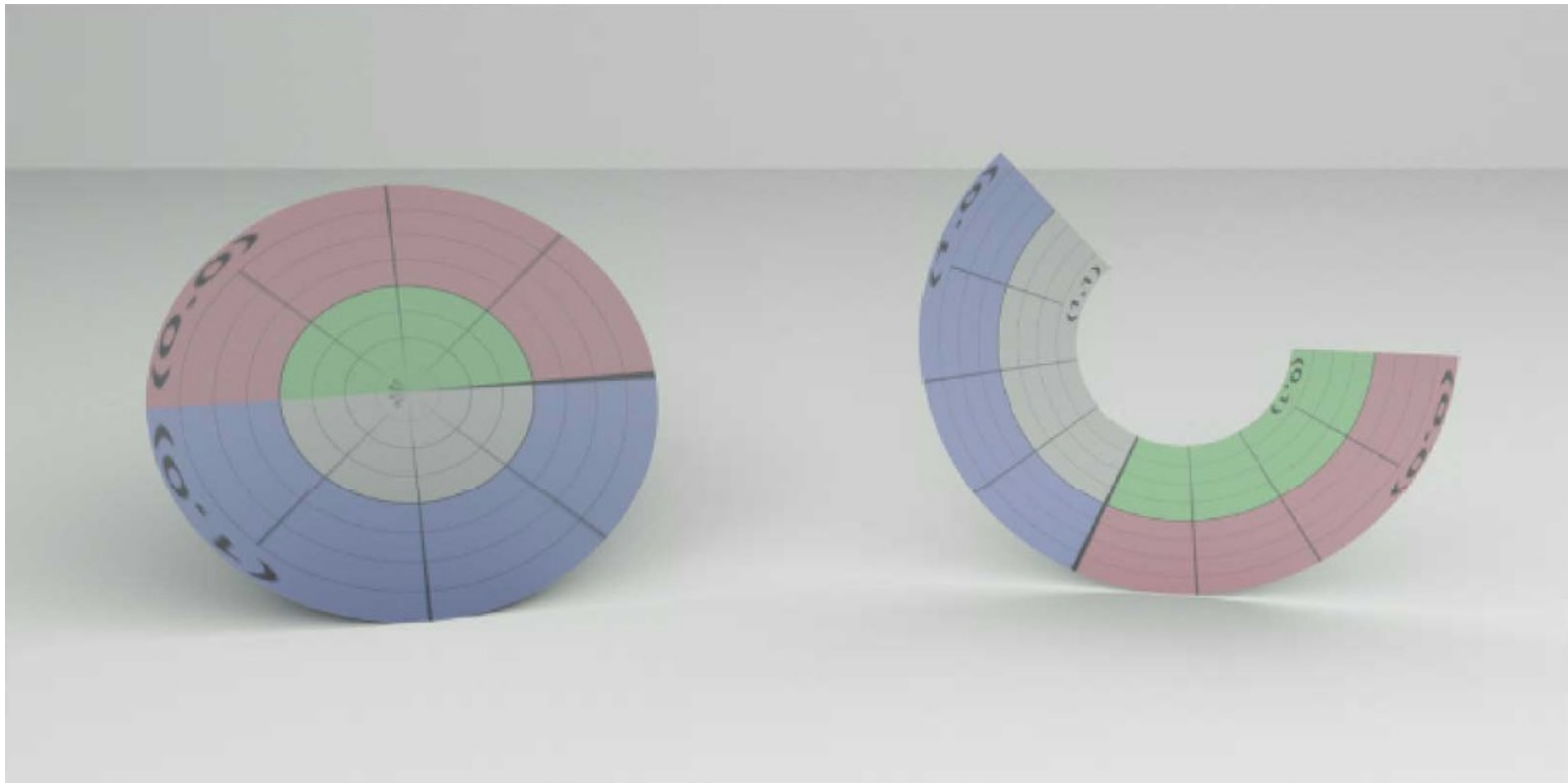
Parametric Surfaces

- **Polar Coordinates**

- $(x, y, 0) = \text{Polar2Cartesian}(r, \varphi)$

- **Disc**

- $p(u, v) = \text{Polar2Cartesian}(R v, 2 \pi u)$ // disc radius R



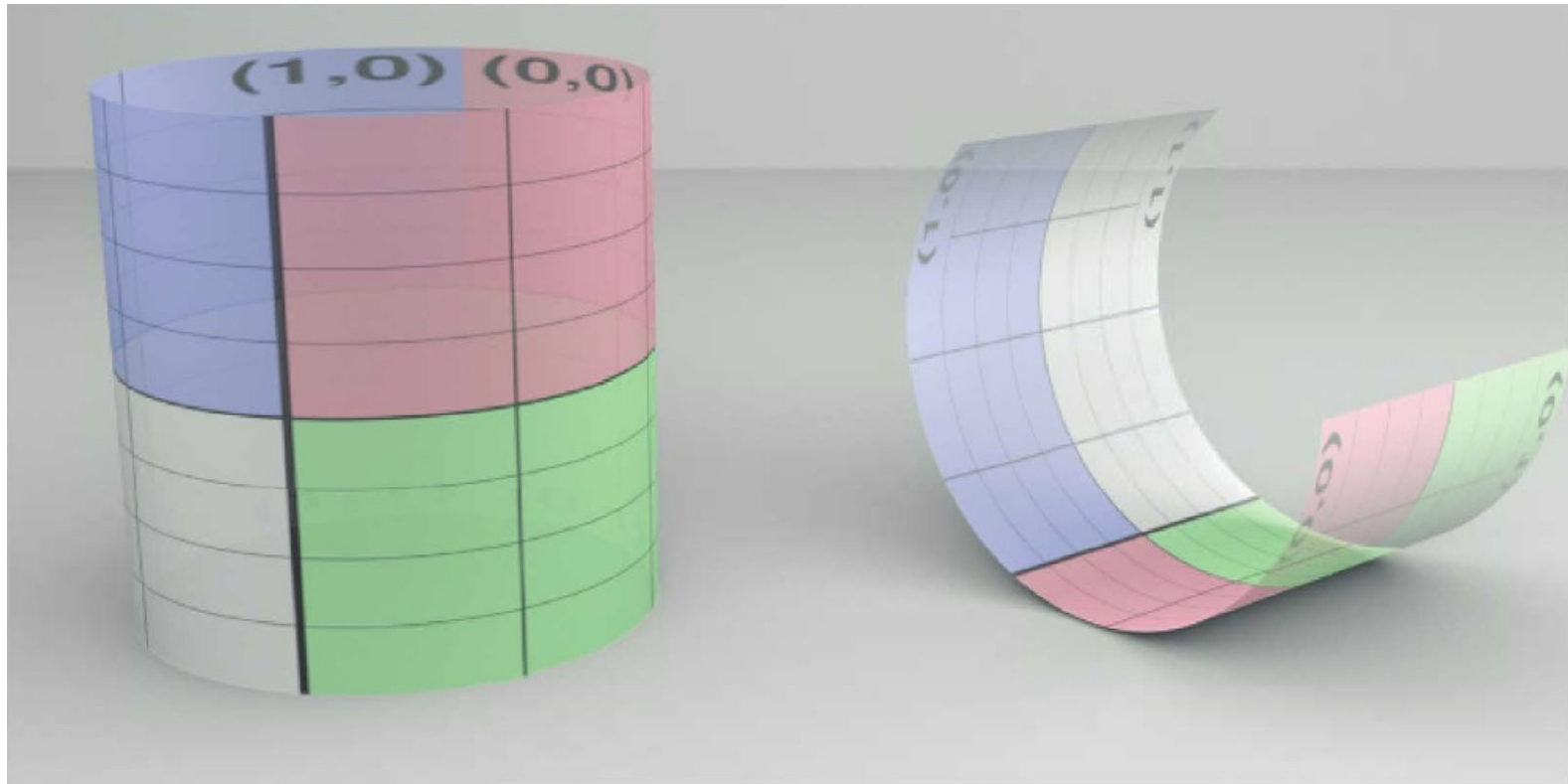
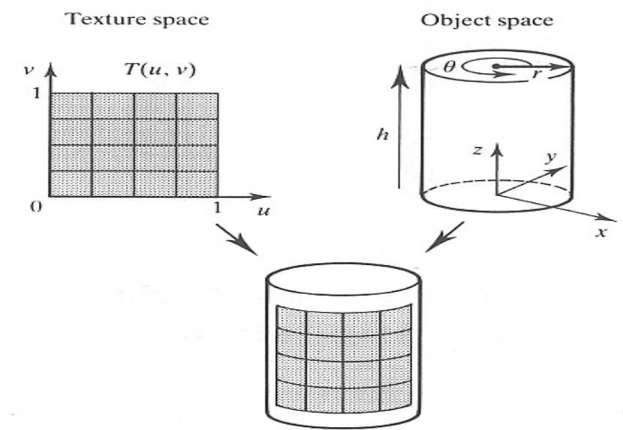
Parametric Surfaces

- **Cylindrical Coordinates**

- $(x, y, z) = \text{Cylindrical2Cartesian}(r, \varphi, z)$

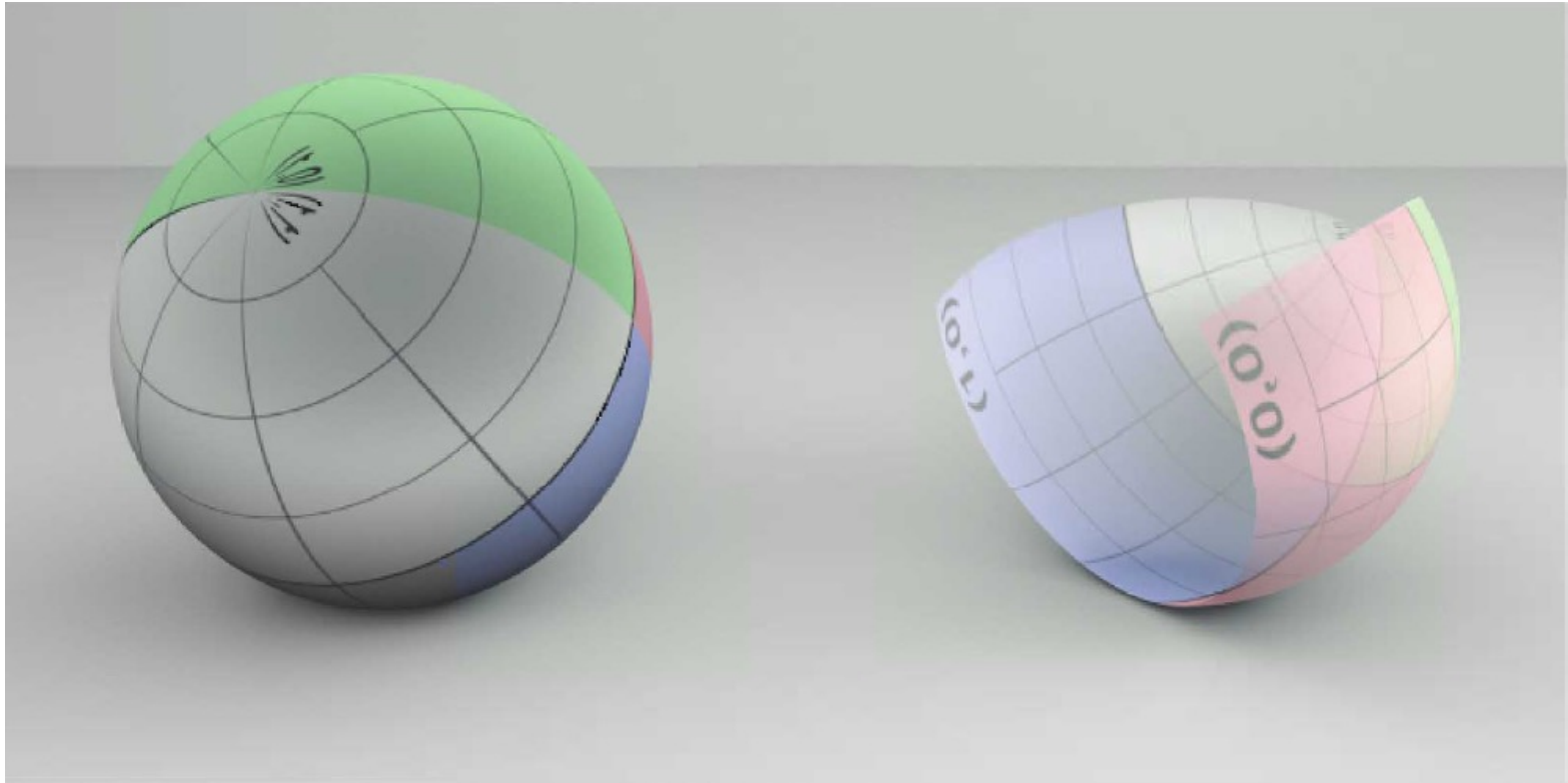
- **Cylinder**

- $p(u, v) = \text{Cylindrical2Cartesian}(r, 2 \pi u, H v)$ // cylinder height H



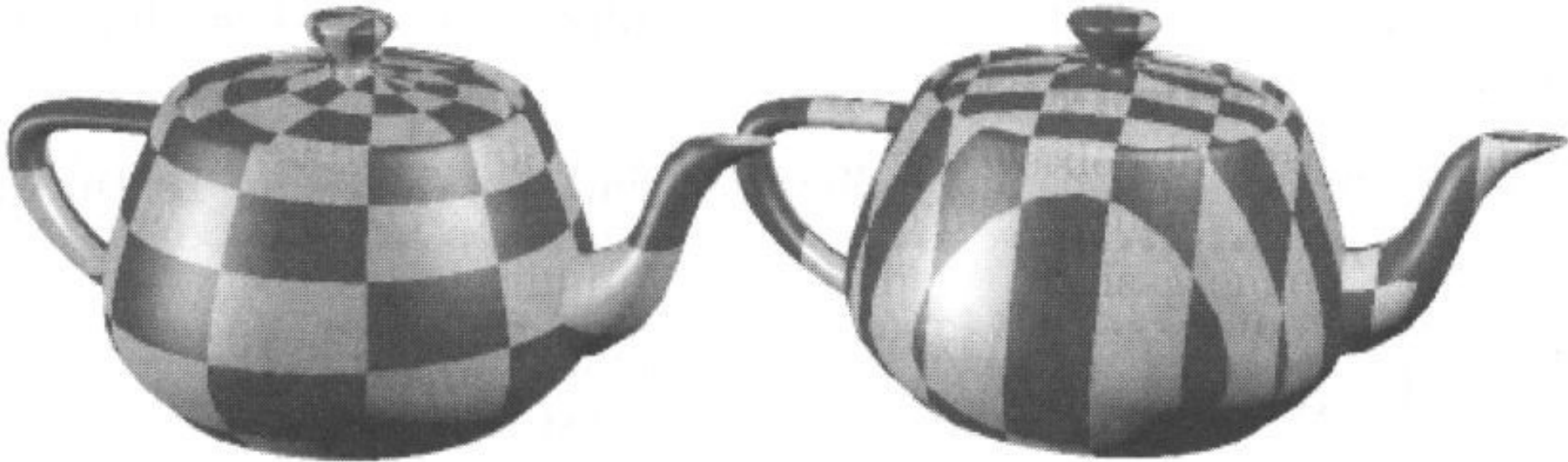
Parametric Surfaces

- **Spherical Coordinates**
 - $(x, y, z) = \text{Spherical2Cartesian}(r, \theta, \varphi)$
- **Sphere**
 - $p(u, v) = \text{Spherical2Cartesian}(r, \pi v, 2 \pi u)$



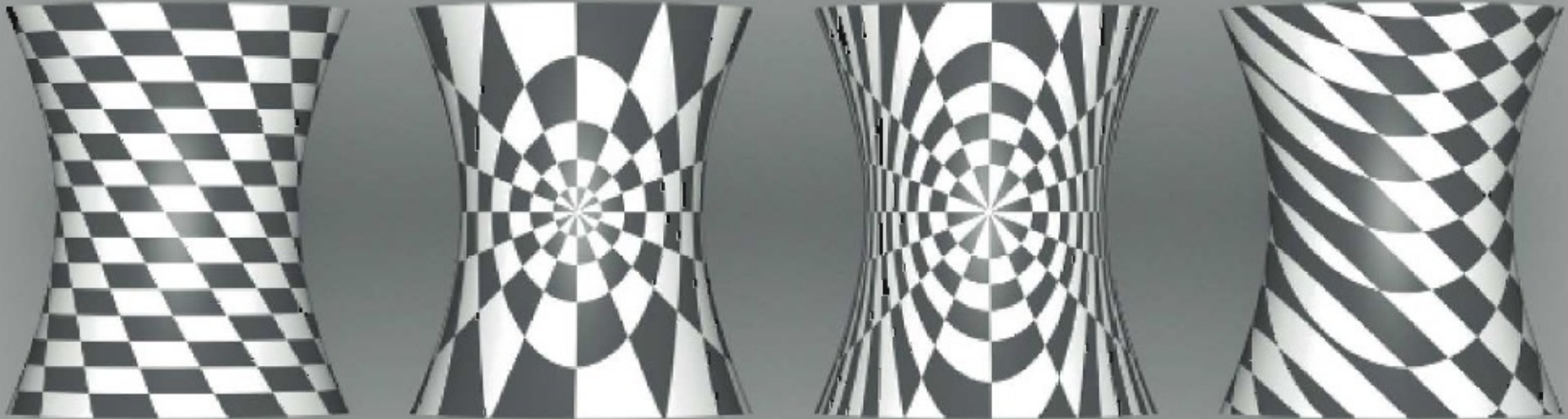
Surface Parameterization

- **Other Surfaces**
 - No intrinsic parameterization??



Intermediate Mapping

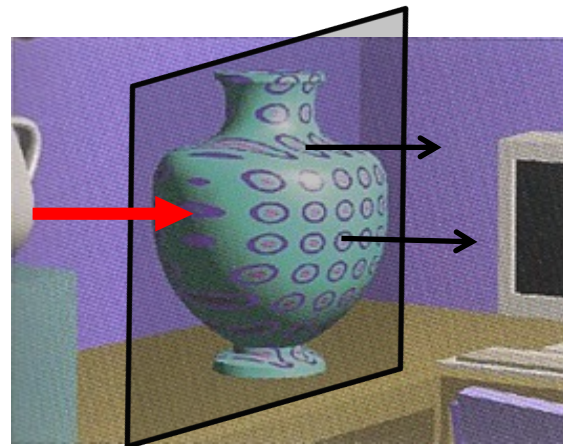
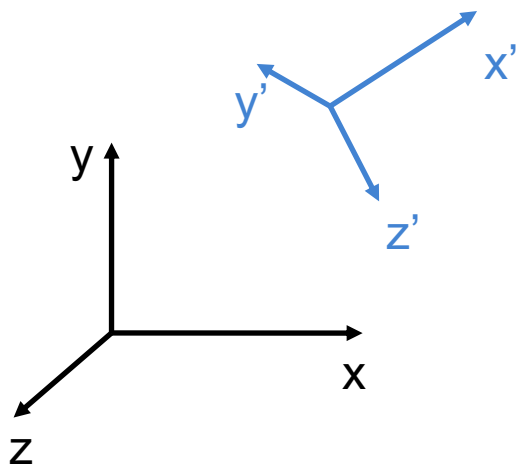
- **Coordinate System Transform**
 - Express Cartesian coordinates into a given coordinate system
- **3D to 2D Projection**
 - Drop one coordinate
 - Compute u and v from remaining 2 coordinates



Intermediate Mapping

- **Planar Mapping**

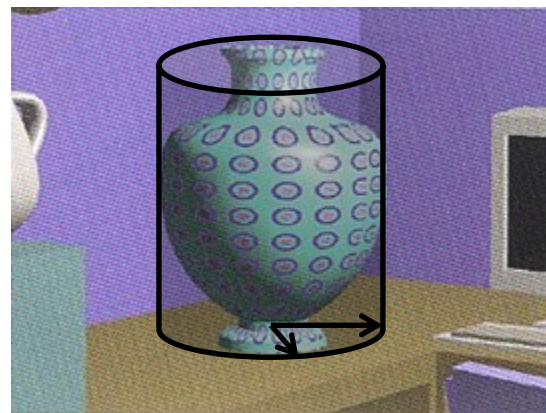
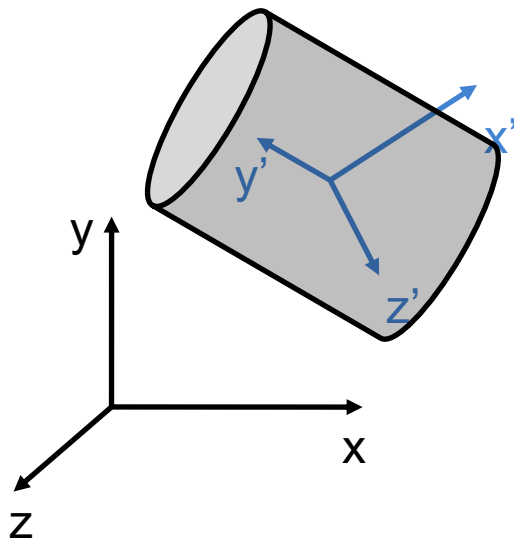
- Map to different Cartesian coordinate system
- $(x', y', z') = \text{AffineTransformation}(x, y, z)$
 - Orthogonal basis: translation + row-vector rotation matrix
 - Non-orthogonal basis: translation + inverse column-vector matrix
- Drop z' , map $u = x'$, map $v = y'$
- E.g.: Issues when surface normal orthogonal to projection axis



Intermediate Mapping

- **Cylindrical Mapping**

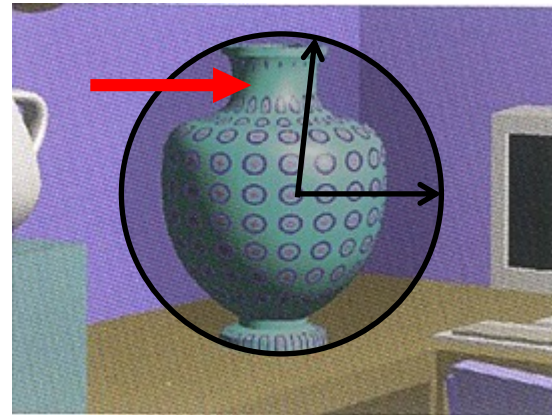
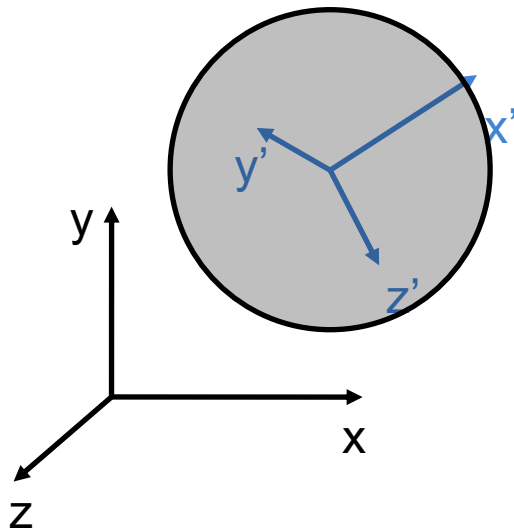
- Map to cylindrical coordinates (possibly after translation/rotation)
- $(r, \varphi, z) = \text{Cartesian2Cylindrical}(x, y, z)$
- Drop r , map $u = \varphi / 2 \pi$, map $v = z / H$
- Extension: add scaling factors: $u = \alpha \varphi / 2 \pi$
- E.g.: Similar topology gives reasonable mapping



Intermediate Mapping

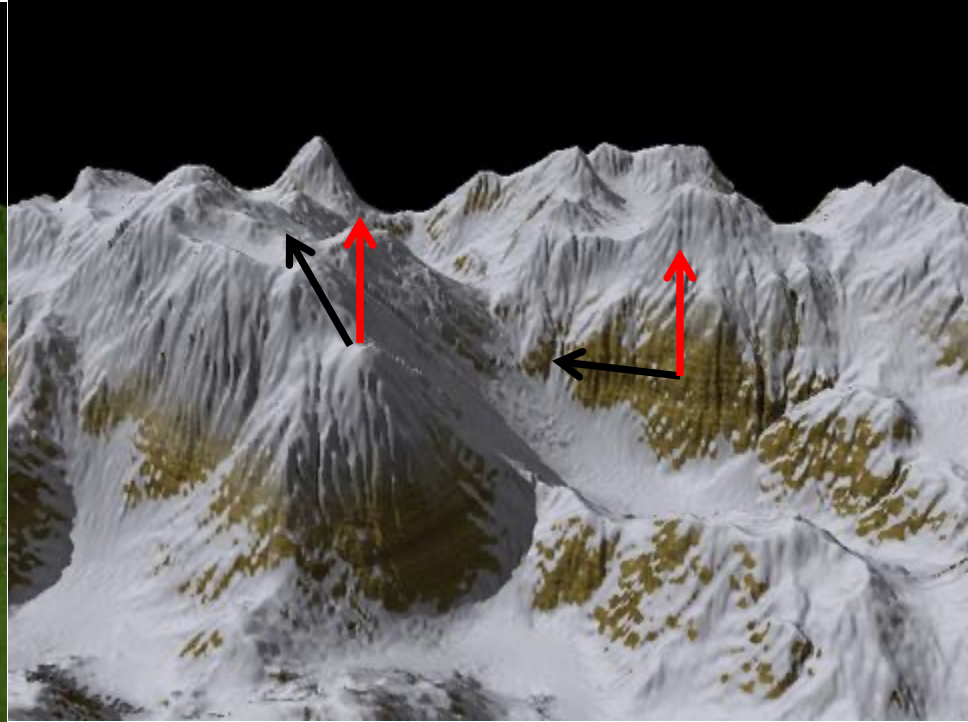
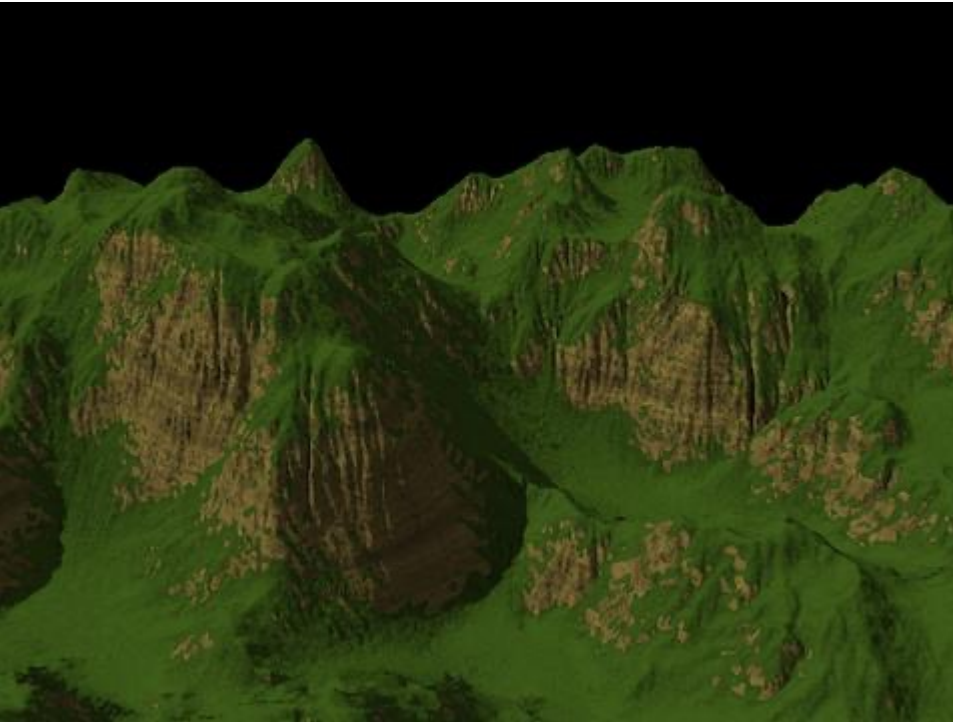
- **Spherical Mapping**

- Map to spherical coordinates (possibly after translation/rotation)
- $(r, \theta, \varphi) = \text{Cartesian2Spherical}(x, y, z)$
- Drop r , map $u = \varphi / 2\pi$, map $v = \theta / \pi$
- Extension: add scaling factors to both u and v
- E.g.: Issues in concave regions



Slope-Based Mapping

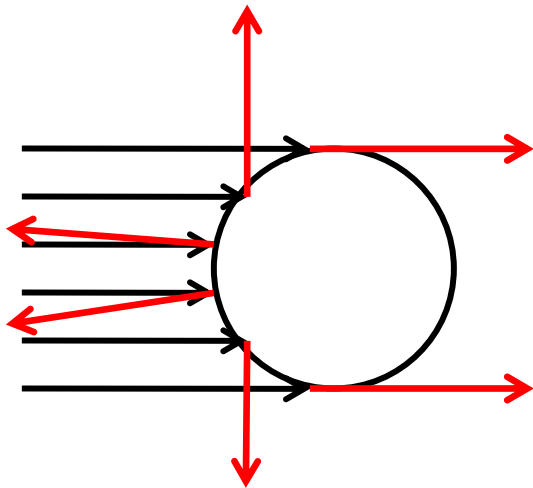
- **Definition**
 - Depends on surface normal and predefined vector
- **Example**
 - $\alpha = n \cdot \omega$
 - return α flatColor + (1 - α) slopeColor;



Environment Map

- **Spherical Map**

- Photo of a reflective sphere (gazing ball)
- Photos with a fish-eye camera



Environment Map

- **Latitude-Longitude Map**

- Remapping 2 images of reflective sphere
- Photo with an environment camera

- **Algorithm**

- Hit infinitely far (parallax-free) background if no intersection found
- Cartesian coords of ray dir. \rightarrow spherical coords \rightarrow uv tex coords



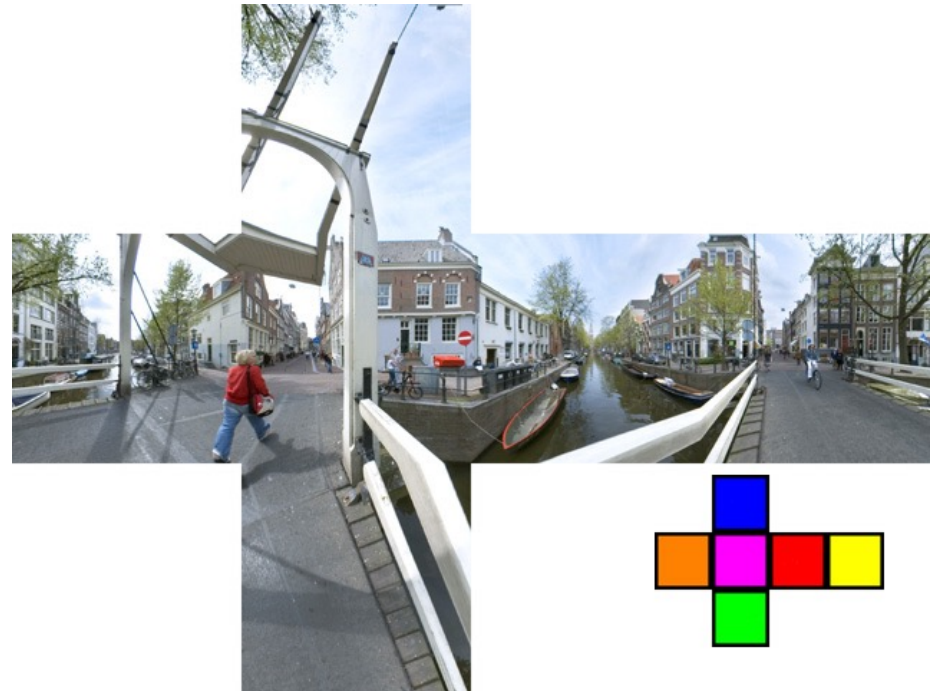
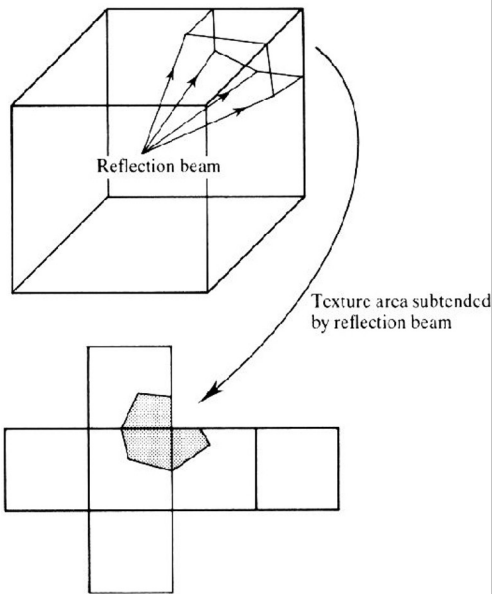
Environment Map

- **Cube Map**

- Remapping 2 images of reflective sphere
- Photos with a perspective camera

- **Algorithm**

- Find main axis (-x, +x, -y, +y, -z, +z) of ray direction
- Use other 2 coordinates to access corresponding face texture
 - Akin to a 90° projective light



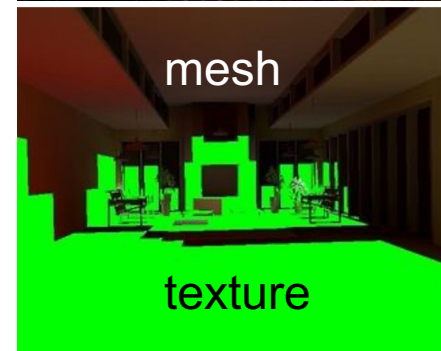
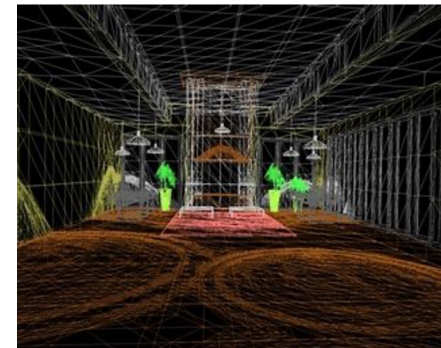
Light Maps

- **Light maps (e.g. in Quake)**
 - Pre-calculated illumination (local irradiance)
 - Often very low resolution: smoothly varying
 - Multiplication of irradiance with base texture
 - Diffuse reflectance only
 - Provides surface radiosity
 - View-independent out-going radiance
 - Animated light maps
 - Animated shadows, moving light spots, etc...



Reflectance Irradiance Radiosity

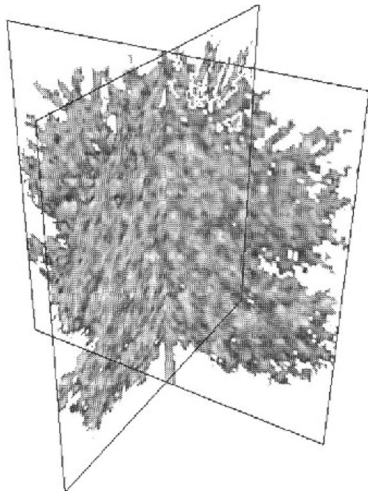
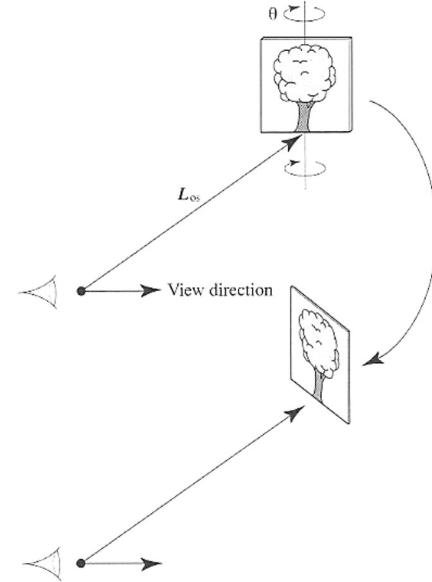
$$B(x) = \rho(x) E(x) = \pi L_o(x)$$



Representing radiosity
in a mesh or texture

Billboards / Transparency Map

- **Single textured polygons**
 - Often with opacity texture
 - Rotates, always facing viewer
 - Used for rendering distant objects
 - Best results if approximately radially or spherically symmetric
- **Multiple textured polygons**
 - Azimuthal orientation: different orientations
 - Complex distribution: trunk, branches, ...



Opacity texture

