## GPU Ray-tracing using Irregular Grids

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Introduction
Ray Tracing with Grids
Challenges

Irregular Grids
Construction (Part I)
Traversal
Construction (Part II)

Results

INTRODUCTION

## Pros

- Very fast parallel construction
- Stackless \& ordered traversal, early exit


## Cons

- Empty space skipping: Teapot in the Stadium
- Cannot minimize both intersections and traversal steps


## INTRODUCTION: UNIFORM GRID



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## Introduction: Uniform Grid



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## INTRODUCTION: UNIFORM GRID



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Redundant
intersections
Empty space


## INTRODUCTION: UNIFORM GRID



Increasing resolution

- Fewer intersections
- More traversal steps


## INTRODUCTION: OUR SOLUTION



Idea: Remove regularity

- Start with a dense subdivision
- Optimize cell shape to minimize traversal cost


## INTRODUCTION: OUR SOLUTION

Uniform Grid: Low Resolution


Traversal steps + Intersections

## INTRODUCTION: OUR SOLUTION

Uniform Grid: Medium Resolution


Traversal steps + Intersections

## INTRODUCTION: OUR SOLUTION

Irregular Grid: Low Resolution


Traversal steps + Intersections

## INTRODUCTION: OUR SOLUTION

Irregular Grid: Medium Resolution


Traversal steps + Intersections

## Introduction: OUR SOLUTION

Irregular Grid: High Resolution


Traversal steps + Intersections

IRREGULAR GRIDS

## Data Structure



## CONSTRUCTION (PART I)

## Initialization

- Initial grid
- Two-level construction:

1. A coarse uniform grid
2. An octree in each of the grid cells

- Adaptive: More effort where the geometry is complex
- Dense: Up to $2^{15}$ resolution in each second-level cell


## CONSTRUCTION (PART I)

Initialization


## CONSTRUCTION (PART I)

## Initialization

- User-defined $\lambda_{1}$ controls top-level resolution
- With scene volume $V$ and number of objects $N$ [Cle+83]:

$$
R_{\{x, y, z\}}=d_{\{x, y, z\}} \sqrt[3]{\frac{\lambda_{1} N}{V}}
$$

- Tries to make cells cubic


## Construction (PART I)

Initialization


## CONSTRUCTION (PART I)

## Initialization

- Octree depth computed independently in each cell
- Same formula, but: $\lambda_{2}$, local number of objects \& volume
- Clamp resolution to a power of two:

$$
D=\left\lceil\log _{2}\left(\max \left(R_{x}, R_{y}, R_{z}\right)\right)\right\rceil
$$

- Compact: only $\log _{2}\left(\log _{2}\left(R_{\max }\right)\right)$ bits needed
- 4 bits = max. resolution of $2^{15} \times 2^{15} \times 2^{15}$


## CONSTRUCTION (PART I)

Initialization


## Construction (PART I)

Initialization


## Construction (Part I): VIrtual Grid



## Property

Cells are aligned on a virtual grid of resolution $R_{x, y, z} 2^{D}$

## Construction (Part I): Voxel Map



Voxel map as a two level grid Memory efficient/Fast lookup

## Traversal

- The data structure is not optimal
- But it can already be used for traversal


## Ideas

- Maintain position on the virtual grid
- Recompute increment along the ray at each step


## INTERLUDE: TRAVERSAL



1. Locate ray origin
2. Loop
2.1 Intersect primitives
2.2 Exit if hit is within cell
2.3 Locate exit point
2.4 Move to next cell

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## Contruction (Part II)

## Traversal Performance

- Poor empty space skipping $\Longrightarrow$ memory latency
- Redundant intersections $\Longrightarrow$ instr./memory latency


## Cell Merging and Expansion

- Local (greedy) optimizations
- Examine cells and their neighborhoods
- Keep optimizations simple and parallelizable


## Contruction (Part II): Optimization Passes



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## Contruction (Part II): Cell Merging



## Cell Merging

- Merge each cell with its neighbor if the SAH decreases:

$$
|\mathcal{R}(A)| \mathcal{S} \mathcal{A}(A)+|\mathcal{R}(B)| \mathcal{S A}(B) \geq|\mathcal{R}(A \cup B)| \mathcal{S} \mathcal{A}(A \cup B)-\mathcal{C}_{t}
$$

- For empty and non-empty cells


## Contruction (Part II): Cell Merging



## Limitations

- Only consider the union of 2 aligned cells
- Union must be a box


## Contruction (Part II): Cell Merging

Stopping criterion

- Keep merging until:

$$
N_{\text {after }} \geq \alpha N_{\text {before }}
$$

- $N_{\text {after }} / N_{\text {before: }}$ number of cells after/before merging
- $\alpha=0.995$


## Contruction (PART II): Optimization Passes



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## Contruction (Part II): Cell Expansion



## Cell Expansion

- Expand the exit boundaries of the cells
- Must maintain correctness of traversal:

$$
\mathcal{R}(B) \subset \mathcal{R}(A)
$$

## Contruction (Part II): Cell Expansion



## Cell Expansion

- Expand the exit boundaries of the cells
- Must maintain correctness of traversal:

$$
\mathcal{R}(A) \not \subset \mathcal{R}(B)
$$

## Contruction (Part II): Cell Expansion



## Limitations

- Must examine every neighbor on the box face
- Binary decision, no partial expansion


## Contruction (Part II): Cell Expansion

## Stopping criterion

- Fixed number of expansion passes:
- 3 for static scenes,
- 1 for dynamic scenes.


## Contruction (PART II): Impact on Traversal



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Results

## Results: Source Code

## GPU implementation

- https://github.com/madmann91/hagrid
- Parallel construction \& traversal
- CUDA implementation
- MIT license


## Results: Static Scenes



## Parameters

- $\left(\lambda_{1}, \lambda_{2}\right)=(0.12,2.4)$ for every scene
- Memory footprint $\approx$ SBVH [SFD09]
- Different viewpoints


## Results: Static Scenes

|  |  |  | Primary (MRays/s) |  | AO (MRays/s) |  | Random (MRays/s) |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Scene | \#Tris | times (ms) | SBVH | Ours | SBVH | Ours | SBVH | Ours |
| Sponza | 262K | 26 | $\begin{aligned} & 409 \\ & 265 \end{aligned}$ | $\begin{aligned} & 653+60 \% \\ & 473+78 \% \end{aligned}$ | $\begin{aligned} & 270 \\ & 187 \end{aligned}$ | $\begin{aligned} & 386+43 \% \\ & 234+25 \% \end{aligned}$ | 166 | $274+65 \%$ |
| Conference | 283K | 22 | $\begin{aligned} & 583 \\ & 523 \end{aligned}$ | $\begin{aligned} & 597+2 \% \\ & 526+1 \% \end{aligned}$ | $\begin{aligned} & 303 \\ & 326 \end{aligned}$ | $\begin{gathered} 332+10 \% \\ 338+4 \% \end{gathered}$ | 295 | $312+6 \%$ |
| Hairball | 2.9 M | 893 | $\begin{gathered} 100 \\ 79 \end{gathered}$ | $\begin{gathered} 148+48 \% \\ 93+18 \% \end{gathered}$ | $\begin{aligned} & 53 \\ & 63 \end{aligned}$ | $\begin{gathered} 69+30 \% \\ 61-3 \% \end{gathered}$ | 19 | $26+37 \%$ |
| Crown | 3.5 M | 203 | $\begin{aligned} & 232 \\ & 181 \end{aligned}$ | $\begin{gathered} 296+28 \% \\ 191+6 \% \end{gathered}$ | $\begin{aligned} & 108 \\ & 112 \end{aligned}$ | $\begin{aligned} & 120+11 \% \\ & 125+12 \% \end{aligned}$ | 221 | $238+8 \%$ |
| San Miguel | 7.9M | 492 | $\begin{aligned} & 227 \\ & 157 \end{aligned}$ | $\begin{aligned} & 291+28 \% \\ & 180+15 \% \end{aligned}$ | $\begin{aligned} & 119 \\ & 125 \end{aligned}$ | $\begin{aligned} & 119+0 \% \\ & 115-8 \% \end{aligned}$ | 119 | 160 + $34 \%$ |

## Results: Build Times vs. Traversal Performance



Varying parameters for Crown

- No local optimum $\neq$ two-level grid
- Increasing density $\Longrightarrow$ increasing performance


## Results: Construction Steps Performance



Time spent during construction

- Average over all static scenes
- Dominated by initialization \& merging


## Results: Dynamic Scenes

## Methodology

- Comparison with two-level grids [KBS11]
- Fixed time budget
- Two-level grids: choose optimal resolution
- Irregular grid:
- Fixed ratio: $\lambda_{1}: \lambda_{2}=1: 8$
- Range: $\lambda_{1} \in[0.01,0.3], \lambda_{2} \in[0.08,2.4]$
- Start at minimum, increase until $T_{\text {build }}=0.5 T_{\text {budget }}$


## Results: DYnamic Scenes



|  | 10FPS (100ms) |  | 20FPS (50ms) |  | 30FPS (33ms) |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 2L Grid | Ours | 2L Grid | Ours | 2L Grid | Ours |
| $\lambda_{1}, \lambda_{2}$ | 0.2, 2.0 | 0.3, 2.4 | 0.2, 2.0 | 0.3, 2.4 | 0.2, 2.0 | 0.3, 2.4 |
| AO spp | 2 | 20 | 1 | 8 | 0 | 3 |

## Results: Dynamic Scenes



## Results: Dynamic Scenes



## Results: CONCLUSION

## Irregular grid properties

- Ordered, stackless traversal
- Same construction/traversal algorithm for:
- Static scenes
- Dynamic scenes
- Performance similar/superior to state-of-the-art


## Future directions

- Exploring initial subdivision schemes
- Different voxel map structure
- More aggressive optimizations


## Thank you!

## Backup: Related Work



Macro regions

|rregular grid
(uniform initialization)

## Macro Regions [Dev89]

- Limited to empty space
- Based on uniform grids


## Backup: Aggressive Optimizations



## Partial expansion

- Expand cells partially over their neighbors
- Test primitives inside neighbor for intersection
- Implemented in GitHub version
- Additional +10-20\% over merge + basic expansion


## References

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